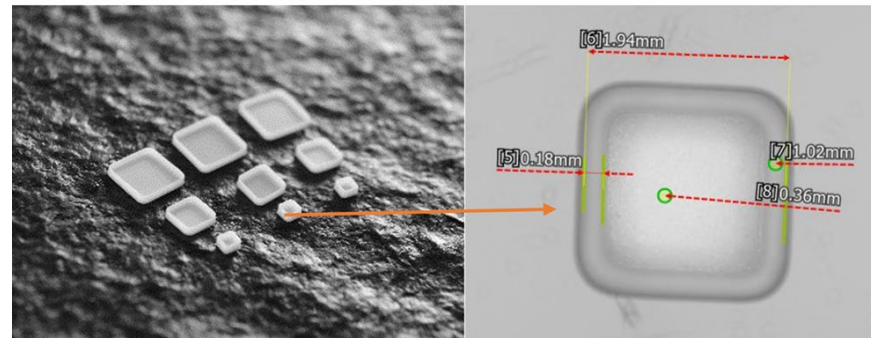
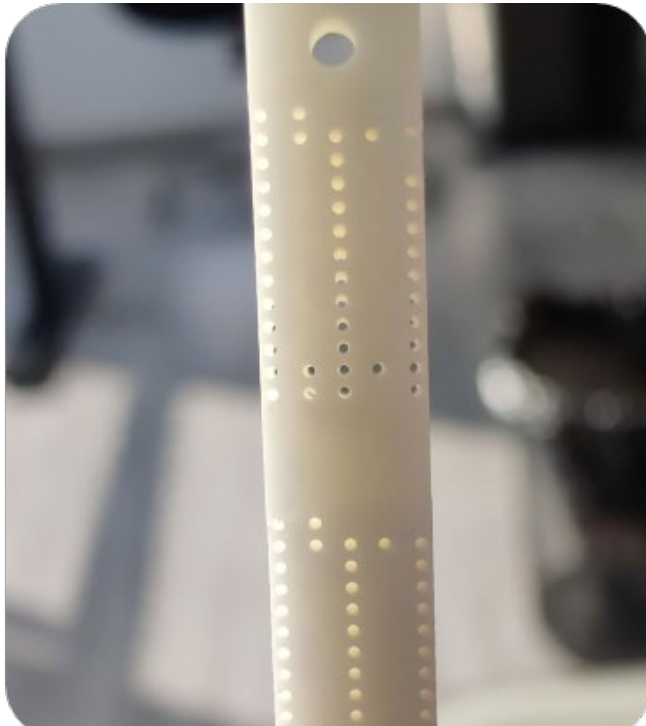


MSE 495 – Advanced Ceramics Technology

Michael Stuer (Empa) - Andrea Testino (PSI)

Week 5 – Perovskites



Perovskites*

Calcium titanate, CaTiO_3 or perovskite¹, is a natural mineral, prototype of a class of mineral with general formula ABX_3 .

This class of materials has interesting properties, such as dielectric, piezoelectric, ferroelectric. In addition, there are examples of magnetic ordering, multiferroic properties, electronic conductivity (even superconductivity) and thermal and optical properties.

They are used in electrode material for SOFC due to high oxide ion conductivity and electron conductivity (and the combination thereof).

In addition, they show catalytic properties and redox behavior.

There are two major aspects that make these class of material interesting:

1. The crystal structure embrace a huge range variants from cubic (such as SrTiO_3), to hexagonal (such as BaNiO_3);
2. The properties can be tune over a wide range by substituting A, B or X. These allow a virtual infinite combination of compounds, including organic molecules, such as methylammonium lead iodine, a class of metal organic perovskites well-known in the recent years for their applications in photovoltaic cells.

Furthermore, thin films, superlattices, and nanoparticles shows unexpected response, when compared to bulk material of the same composition.

* R.J.D. Tilley "Perovskites. Structure-Property Relationship", Wiley, 2016 (ISBN: 9781118935668)

¹ Russian mineralogist Count Lev Aleksevich von Petrovski

Mercury: crystal structure visualization

Software download: <https://www.ccdc.cam.ac.uk/solutions/software/free-mercury/>

Brief introduction on View Symmetry Elements and Operation <https://youtu.be/umx-CcRFDds>

List of space groups: https://en.wikipedia.org/wiki/List_of_space_groups

Cubic, Pm-3m (221)



Hexagonal, P6₃/mmc (194)

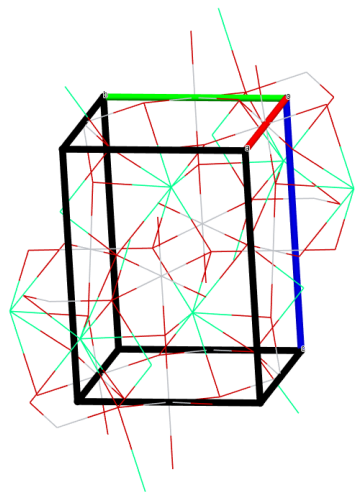


Tetragonal, P4mm (99)

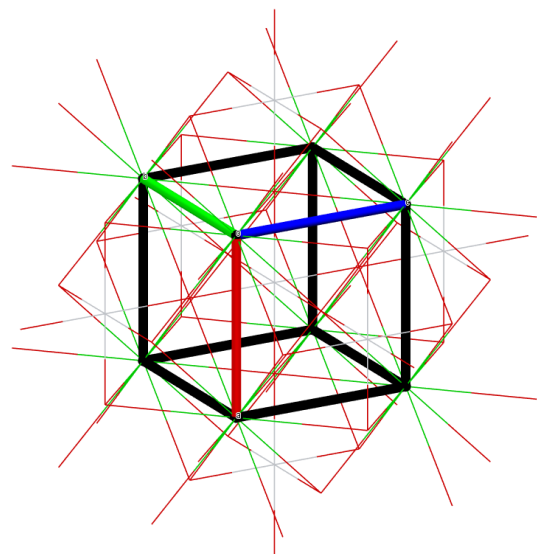


Orthorhombic, Pbnm (62)

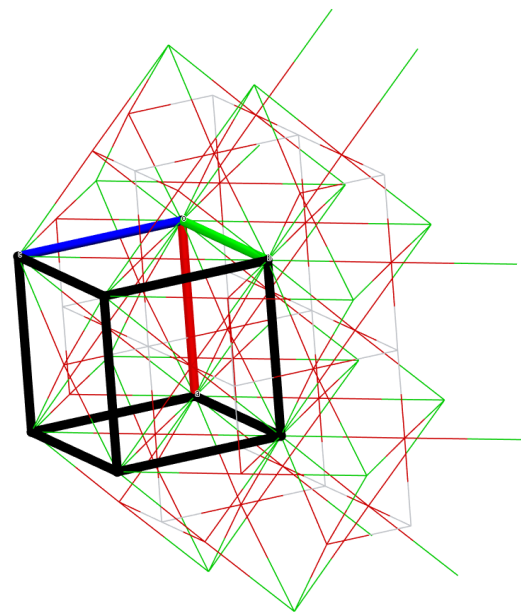




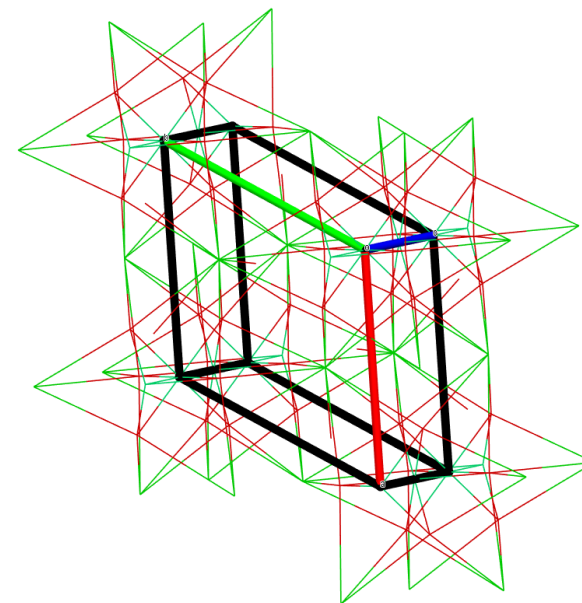
CaTiO₃, Orthorhombic



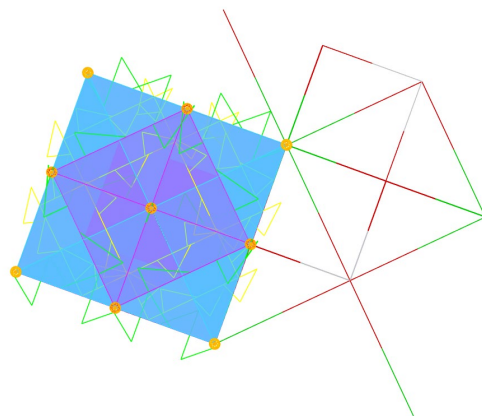
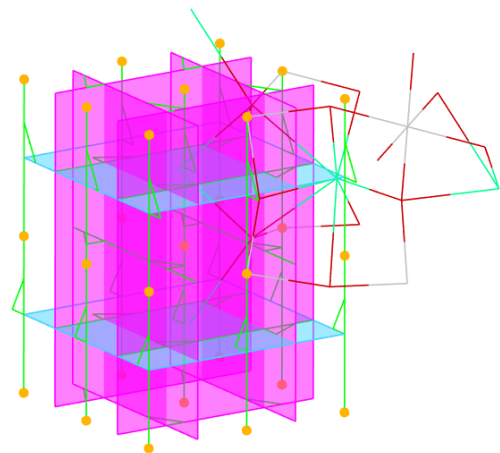
SrTiO₃, BaTiO₃, cubic



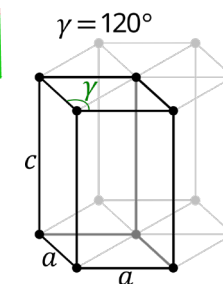
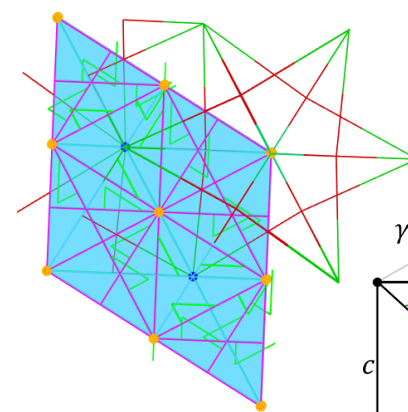
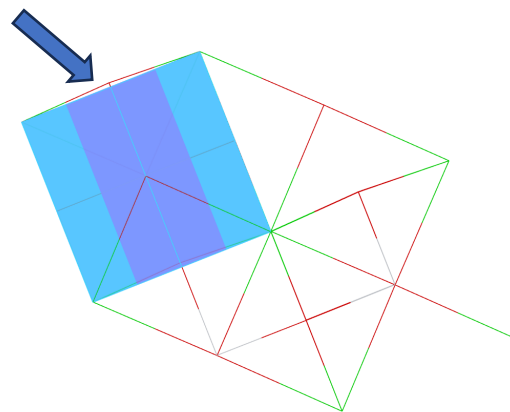
BaTiO₃, tetragonal



BaNiO₃, Hexagonal₄



distortion



Assuming simple ionic compounds, we might have

A, B = 1, 2 with X= -1

A, B = 1, 5 with X= -2
2, 4
3, 3

A, B = 4, 5 with X= -3

where usually

A is a large-size cation and (Ca, Ba, Sr, ...)

B is a mediums-size cation (Ti, Zr, Ni, ...)

X anion (O, halogen, ...)

giving a neutral ionic structure.

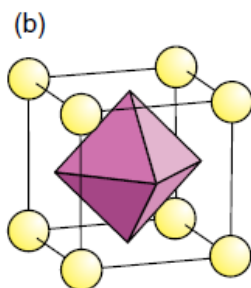
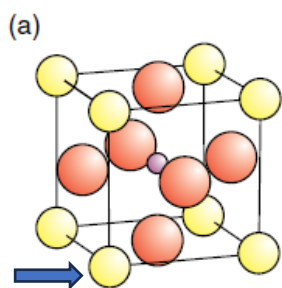
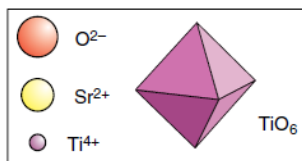
Table 1.1 Representative ABX_3 perovskite phases^a

Phase	Space group ^b	Unit cell		
		a (nm)	b (nm)	c (nm)
1, 2				
AgMgF ₃	C, $Pm\bar{3}m$ (221)	0.41162		
CsPbI ₃	C, $Pm\bar{3}m$ (221)	0.62894		
KCuF ₃	T, $I4/mcm$ (140)	0.56086		0.76281
KMgF ₃	C, $Pm\bar{3}m$ (221)	0.39897		
KZnF ₃	C, $Pm\bar{3}m$	0.40560		
NaMgF ₃	O, $Pbnm$ (62)	0.48904	0.52022	0.71403
NaFeF ₃	O, $Pnma$ (62)	0.56612	0.78801	0.54836
NH ₄ ZnF ₃	C, $Pm\bar{3}m$ (221)	0.41162		
1, 5				
KTaO ₃	C, $Pm\bar{3}m$ (221)	0.40316		
KNbO ₃	O, $Amm2$ (38)	0.3971	0.5697	0.5723
2, 4				
SrTiO ₃	C, $Pm\bar{3}m$ (221)	0.3905		
BaTiO ₃	T, $P4mm$ (99)	0.39906		0.40278
CaTiO ₃	O, $Pbmn$ (62)	0.54035	0.54878	0.76626
BaSnO ₃	C, $Pm\bar{3}m$ (221)	0.4117		
CdSnO ₃	O, $Pnma$ (62)	0.52856	0.74501	0.51927
CaIrO ₃	O, $Pbnm$ (62)	0.52505	0.55929	0.76769
PbTiO ₃	T, $P4mm$ (99)	0.3902		0.4143
PbZrO ₃	O, $Pbam$ (55)	0.58822	1.17813	0.82293
SrCoO ₃	C, $Pm\bar{3}m$ (221)	0.3855		
SrMoO ₃	C, $Pm\bar{3}m$ (221)	0.39761		
SrRuO ₃	O, $Pnma$ (62)	0.55328	0.78471	0.55693
(Fe,Mg)SiO ₃	O, $Pnma$ (62)	0.5020	0.6900	0.4810
3, 3				
BiFeO ₃	Tr, $R3c$ (161)	0.55798		1.3867
BiInO ₃	O, $Pnma$ (62)	0.59546	0.83864	0.50619
ErCoO ₃	O, $Pbnm$ (62)	0.51212	0.54191	0.73519
GdFeO ₃	O, $Pbnm$ (62)	0.53490	0.56089	0.76687
HoCrO ₃	O, $Pnma$ (62)	0.5518	0.7539	0.5245
LaAlO ₃	Tr, $R3c$ (161)	0.53644		1.31195
LaCoO ₃	Tr, $R\bar{3}c$ (167)	0.54437		1.30957
LaMnO ₃	O, $Pbnm$ (62)	0.55367	0.57473	0.76929
LaTiO ₃	O, $Pbnm$ (62)	0.5576	0.5542	0.7587
NdAlO ₃	Tr, $R\bar{3}c$ (167)	0.53796		1.31386
PrRuO ₃	O, $Pnma$ (62)	0.58344	0.77477	0.53794
YbMnO ₃	O, $Pbnm$ (62)	0.52208	0.58033	0.73053
4, 5				
ThTaN ₃	C, $Pm\bar{3}m$	0.4020		

^a Many of these phases are polymorphic, and lattice parameters vary with temperature and pressure.

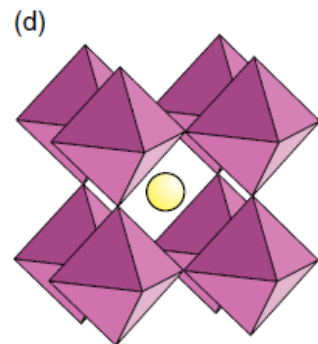
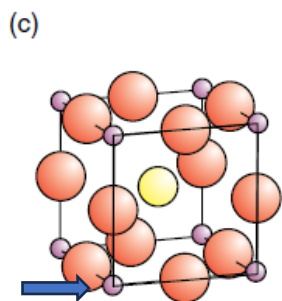
^b The crystal system, here and throughout the other tables in this book, is abbreviated thus: C, cubic; H, hexagonal; M, monoclinic; O, orthorhombic; T, tetragonal; Tr, trigonal (often specified in terms of a hexagonal unit cell); Tri, triclinic.

SrTiO₃ – the aristotype* perovskite



Origin on Sr²⁺

Sr: 1 (a) 0,0,0;
 Ti: 1 (b) ½,½,½;
 O: 3 (c) ½,½,0; ½,0,½; 0,½,½;

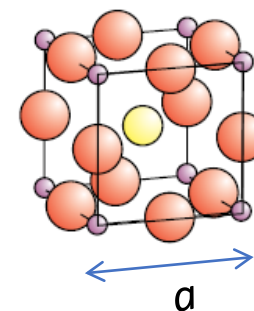


Origin on Ti⁴⁺

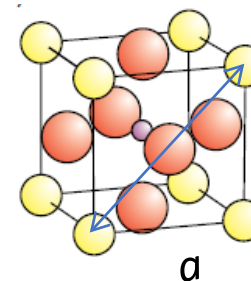
Ti: 1 (a) 0,0,0;
 Sr: 1 (b) ½,½,½;
 O: 3 (d) ½,0,0; 0,½,0; 0,0,½;

Sr²⁺ is coordinated with 12 O²⁻

Ti⁴⁺ is coordinated with 6 O²⁻



$$2(B - X) = a$$



$$2(A - X) = \sqrt{2}a$$

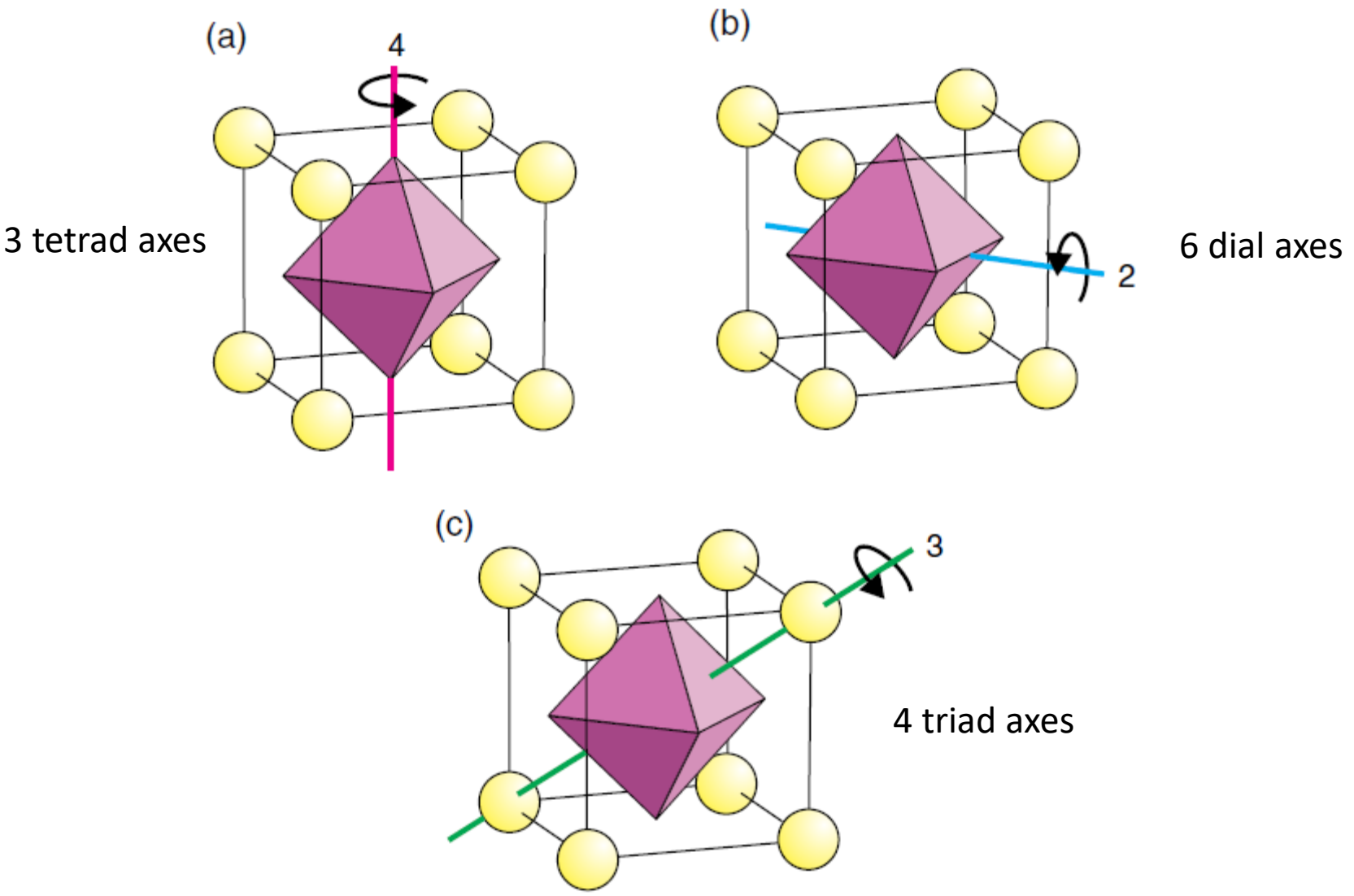
$$\frac{(A - X)}{\sqrt{2}(B - X)} = 1$$

Goldschmidt, 1926

A-X : bond distance A – X

B-X : bond distance B – X

Symmetry axes



The Goldschmidt tolerance factor (t)

In order to evaluate the tolerance factor, the ionic radii are needed.

$$\frac{(A - X)}{\sqrt{2}(B - X)} = 1$$

$$t = \frac{(r_A + r_X)}{\sqrt{2}(r_B + r_X)}$$

Where r_A is the radius of the cage site cation, r_B is the radius of the octahedrally coordinated cation, and r_X is the radius of the anion.

Goldschmidt proposed that a perovskite structure would form if $t \approx 1$

To make this estimation, it is necessary to use the radii of the appropriate coordination*, which has to be 12 for A, 6 for B, and linear (2) for X.

Since many perovskites are described, it is in use to consider the bond lengths in the crystal structure rather than the ionic radii and consider the observed tolerance factor:

$$t_{obs} = \frac{(A - X)}{\sqrt{2}(B - X)}$$

It is a simple but powerful method. If t is in the range 0.9 - 1 a cubic perovskite structure is plausible. For $t > 1$, hexagonal packing is preferred. For $0.7 < t < 0.9$, lower symmetry can be predicted. This works reasonably well for oxides. For chlorides and sulphides, the t values are lower with cubic structure for $t = 0.8-0.9$.

*https://en.wikipedia.org/wiki/Coordination_geometry

The Goldschmidt tolerance factor (t)

For complex perovskites, e.g., with different cations in A-site and different cation in B-site, the average bond lengths can be considered.

$$t_{obs} = \frac{\langle A - X \rangle}{\sqrt{2} \langle B - X \rangle}$$

In addition to the coordination*, the ionic radii dependent on the spin state** for the metals from Cr to Ni.

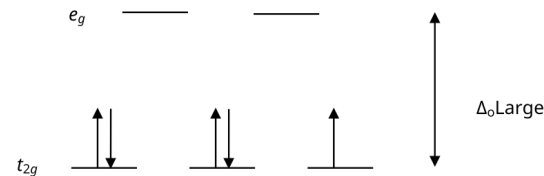
For instance: Fe³⁺

Fe electronic configuration: 4s² 3d⁶

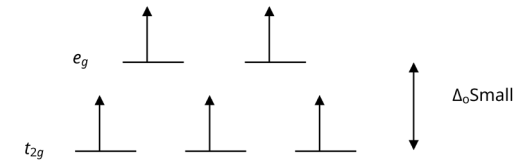
Fe³⁺ electronic configuration : 4s⁰ 3d⁵

Fe³⁺, coord. 6, low spin = 55 pm

Fe³⁺, coord. 6, high spin = 64.5 pm



Low spin



High spin

* https://en.wikipedia.org/wiki/Ionic_radius

** [https://en.wikipedia.org/wiki/Spin_states_\(d_electrons\)](https://en.wikipedia.org/wiki/Spin_states_(d_electrons))

Electroceramics: concepts recall

Dielectric: insulator that can be polarized by an applied electric field (linear)

Paraelectric: non-linear P vs. E (centrosymmetric structures)

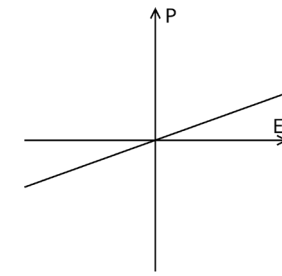
Ferroelectric: in analogy with ferromagnetic material, is a material that have a spontaneous electric polarization that can be reversed by the application of an external electric field. They show hysteresis.

Piezoelectric materials: applying a displacement we got a potential; applying a potential we got a displacement. E.g., lead zirconate titanate, (PZT, $\text{Pb}(\text{Ti,Zr})\text{O}_3$) or lead-free ceramics, potassium sodium niobate, (KNN, (K, Na) NbO_3 -based) materials.

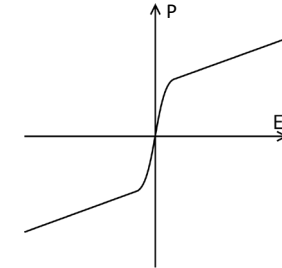
Pyroelectric materials (thermoelectric): applying a potential, we got a heat (cool) flow; applying a heat flow, we got a potential, e.g., lithium tantalate (LiTaO_3).

If a material shows ferroelectric and ferromagnetic properties is called multiferroic.

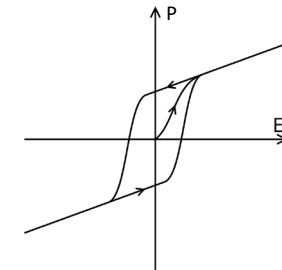
Typically, material demonstrate ferroelectricity only below a certain temperature, called Curie temperature, T_c . They become paraelectric above T_c .



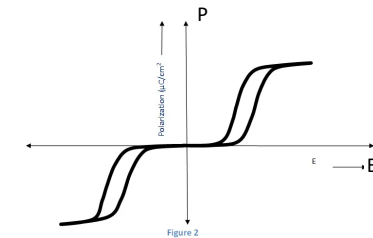
Dielectric



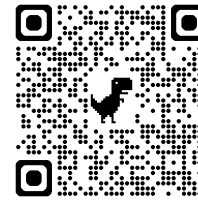
Paraelectric



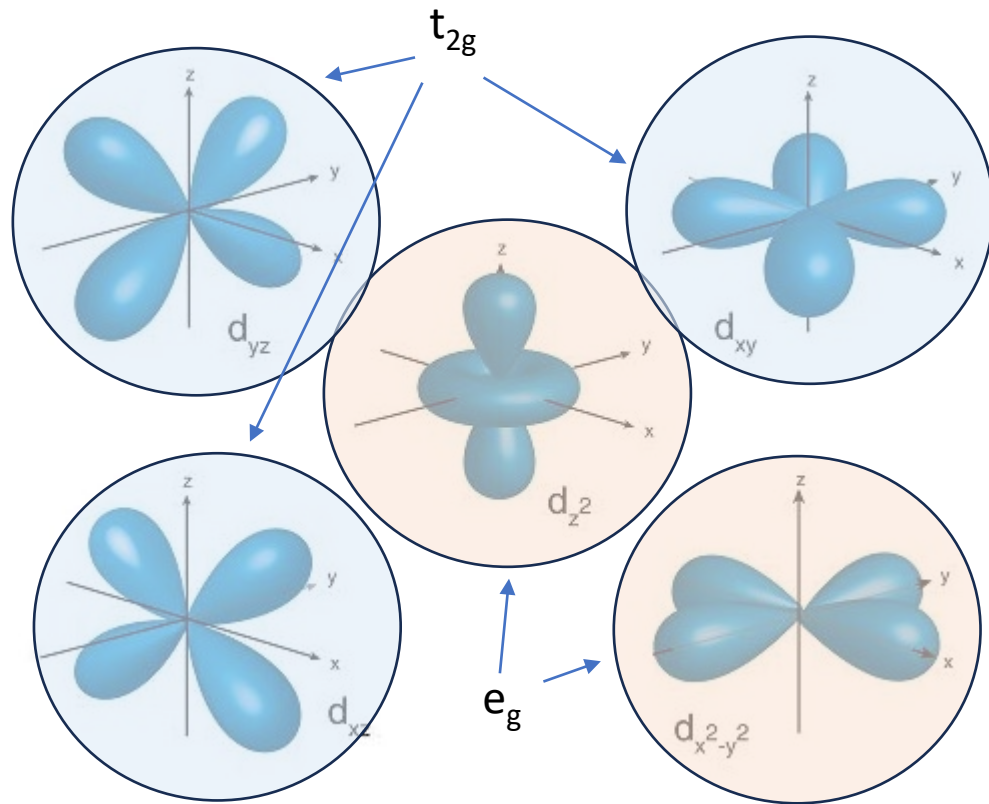
Ferroelectric



Antiferroelec.

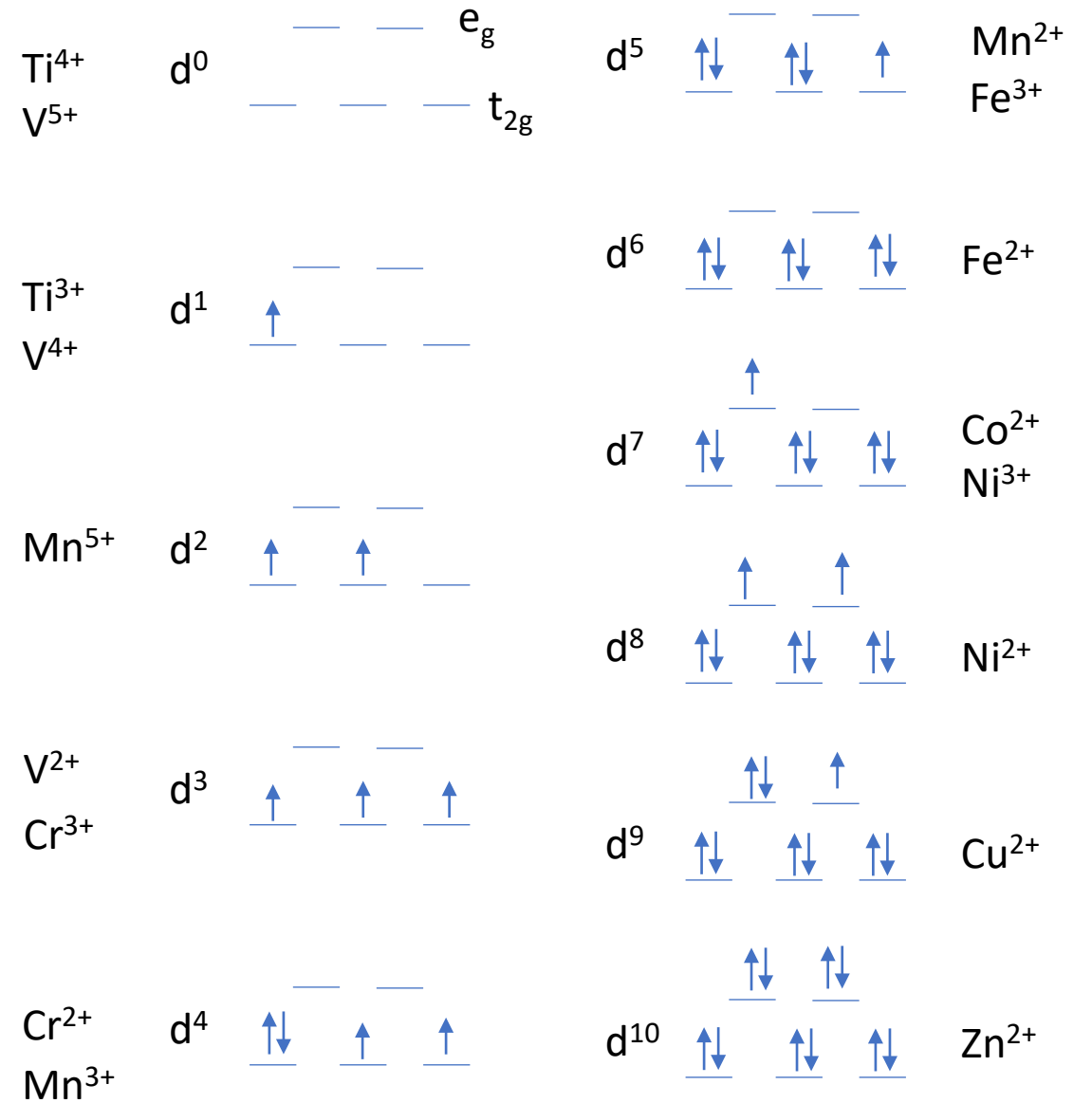


Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
Period ↓																			
1	1 H																	2 He	
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne	
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
6	55 Cs	56 Ba	57 La	*	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
7	87 Fr	88 Ra	89 Ac	*	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
				*	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	
				*	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	



1. d orbitals "shape"

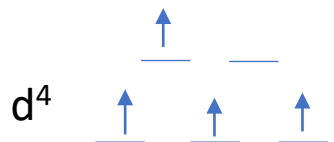
Sodium 22.990	Magnesium 24.305	IIIB 3B	IVB 4B	VB 5B	VIB 6B	VII B 7B	VIII 8	IB 1B	II B 2B	Alum. 26.98		
19 K Potassium 39.098	20 Ca Calcium 40.078	21 Sc Scandium 44.956	22 Ti Titanium 47.88	23 V Vanadium 50.942	24 Cr Chromium 51.996	25 Mn Manganese 54.938	26 Fe Iron 55.833	27 Co Cobalt 58.933	28 Ni Nickel 58.693	29 Cu Copper 63.546	30 Zn Zinc 65.39	31 Ga Gallium 69.723
37 Rb Rubidium 85.468	38 Sr Strontium 87.62	39 Y Yttrium 88.906	40 Zr Zirconium 91.224	41 Nb Niobium 92.906	42 Mo Molybdenum 95.94	43 Tc Technetium 98	44 Ru Ruthenium 101.07	45 Rh Rhodium 102.905	46 Pd Palladium 106.36	47 Ag Silver 107.868	48 Cd Cadmium 112.411	49 In Indium 114.818



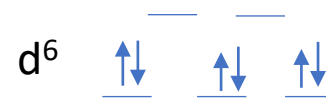
2. Hund's and Pauli's rules



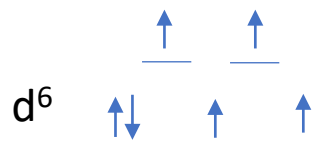
Low spin
 t_{2g} degeneration



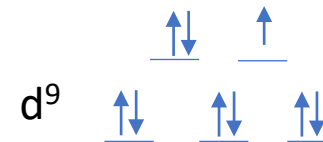
High spin
 e_g degeneration



ls



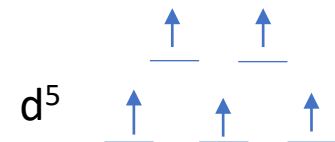
hs
 t_{2g} deg.



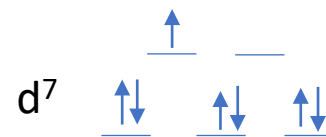
e_g deg.



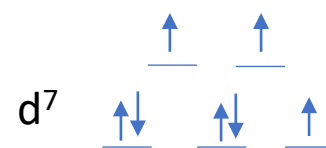
ls
 t_{2g} deg.



hs



ls
 e_g deg.

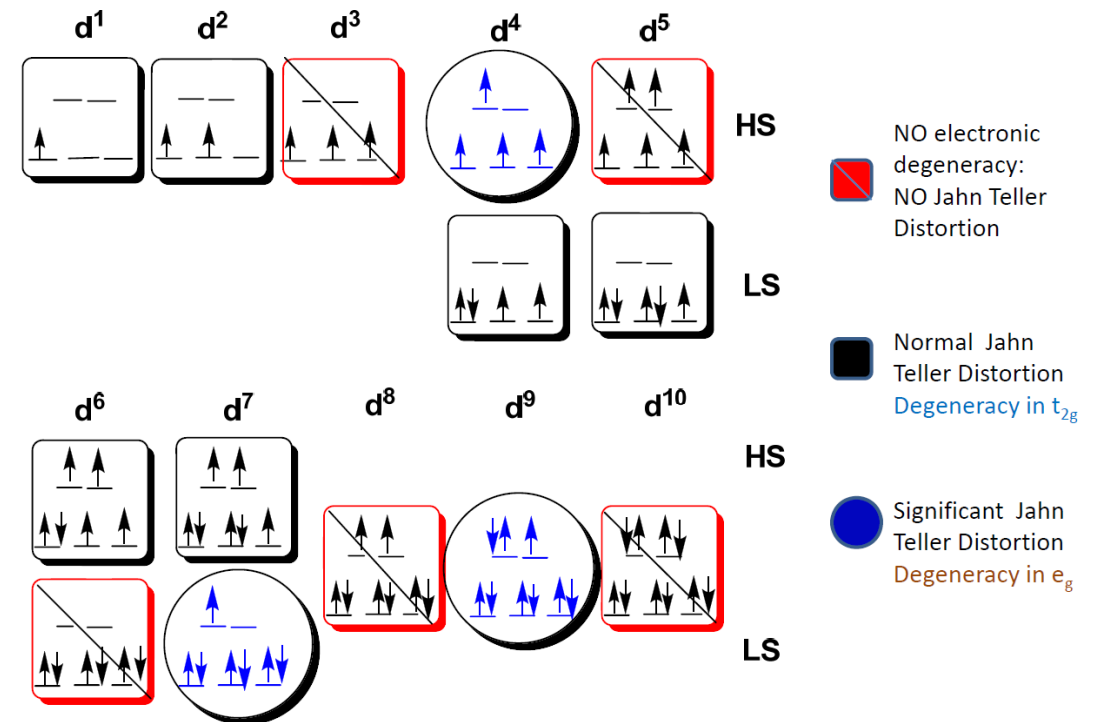
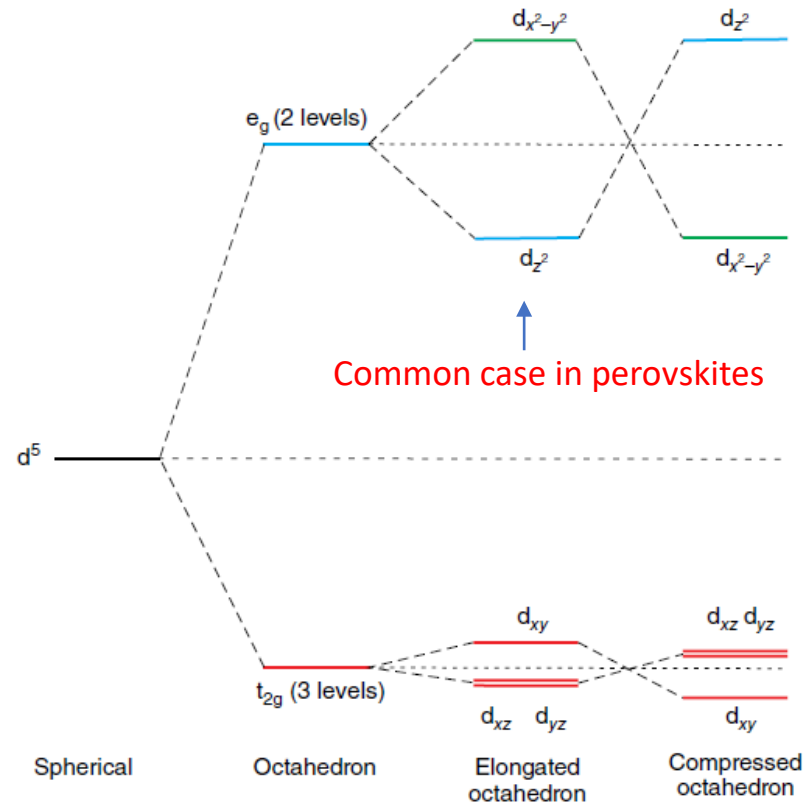


hs
 t_{2g} deg.

Jahn-Teller distortion (first order) – applied to octahedrally coordinated transition metal **B-site** cations

Jahn–Teller theorem*: “Any molecule with a symmetrical atomic configuration and a degenerate electronic ground state is unstable and will distort so as to remove the electronic degeneracy.”

In the spherical field, the 5 d orbitals have the same energy level. In an octahedral field, the degeneracy is reduced, giving 2 energy levels: e_g (2 levels) and t_{2g} (3 levels). When electrons occupy these levels, we might have degeneracy in the e_g (with significant distortion) and t_{2g} (not significant distortion).



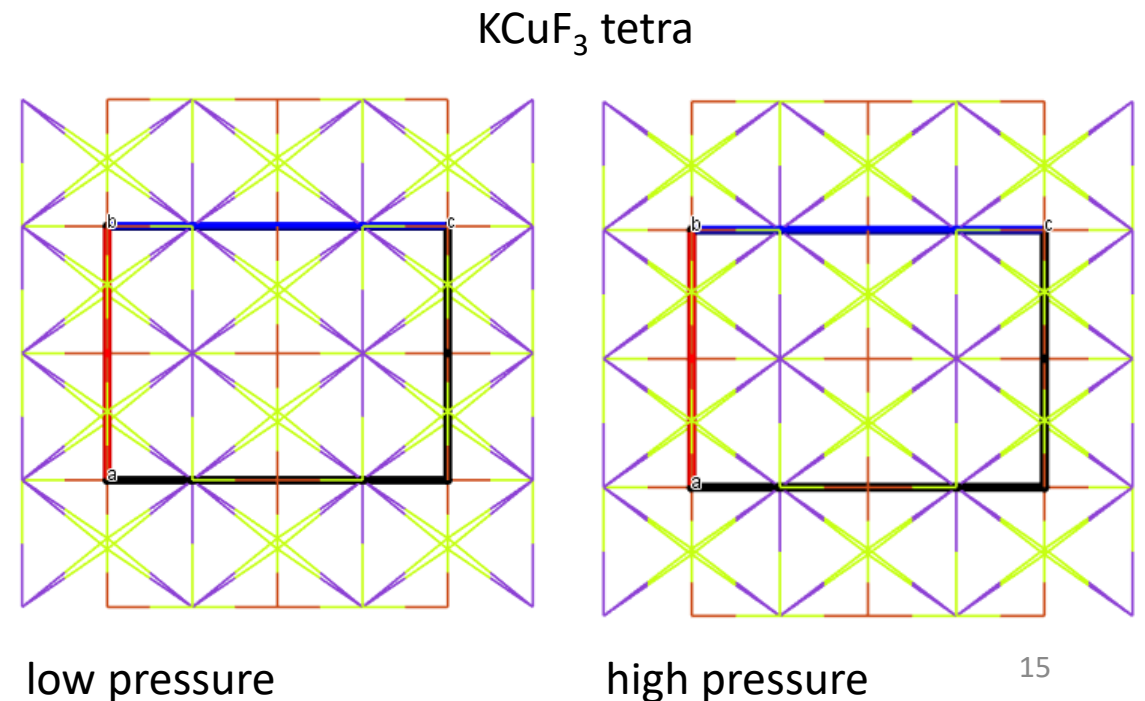
*H. Jahn and E. Teller (1937). "Stability of Polyatomic Molecules in Degenerate Electronic States. I. Orbital Degeneracy". Proceedings of the Royal Society A 161 (905): 220–235

Jahn-Teller distortion (first order) – applied to octahedrally coordinated transition metal **B-site** cations

A cation with odd number of electron in the e_g level, for instance Cr^{2+} (hs), Co^{2+} (ls), or Cu^{2+} will undergo distortion, compression or elongation, along one of the equivalent tilt axis. The energy difference in t_{2g} is rather small, may induce a negligible distortion. Instead, in the e_g case is significant and does lead to distortion. In perovskite, the distortion is generally elongation. This distortion does not influence, in general, the A and B positions but the cell symmetry drops to tetragonal or orthorhombic.

The J-T distortion is temperature and pressure sensitive, so high pressure and/or high temperature contrast the distortion, promoting the high symmetry configuration (cubic).

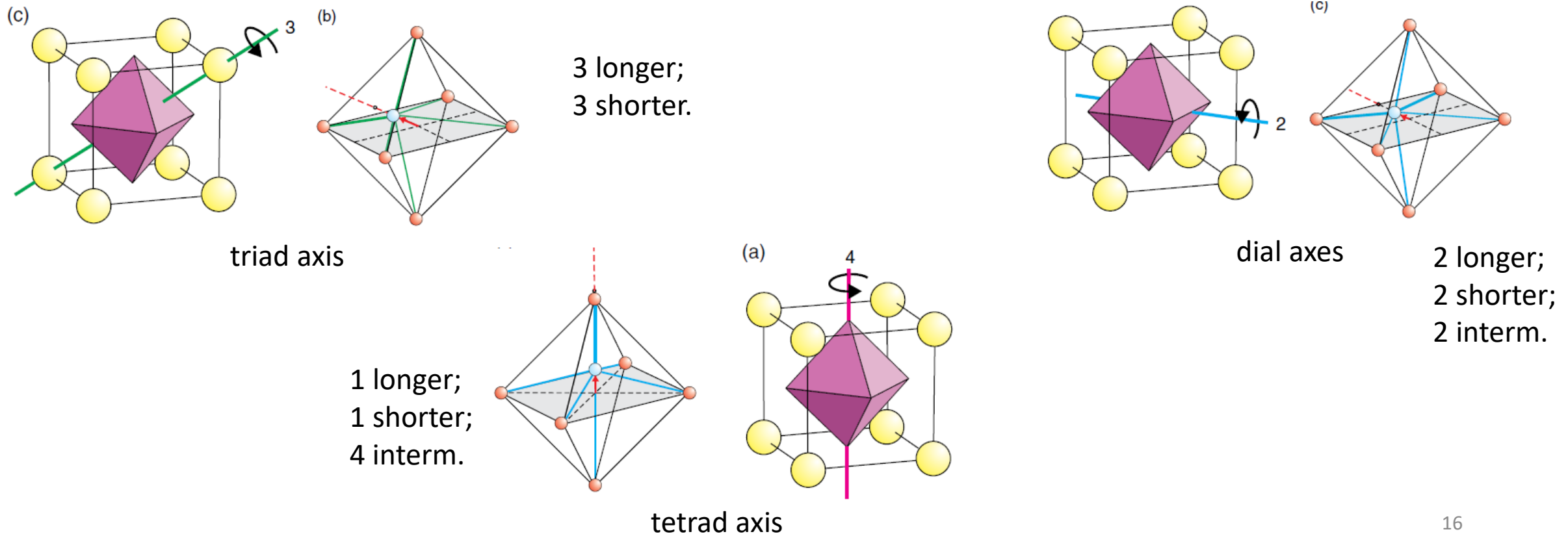
An example is given by KCuF_3 . The J-T ion Cu^{2+} show degeneration of the e_g level. It is tetragonal at 295K and ambient pressure. At high pressure the distortion decreases.



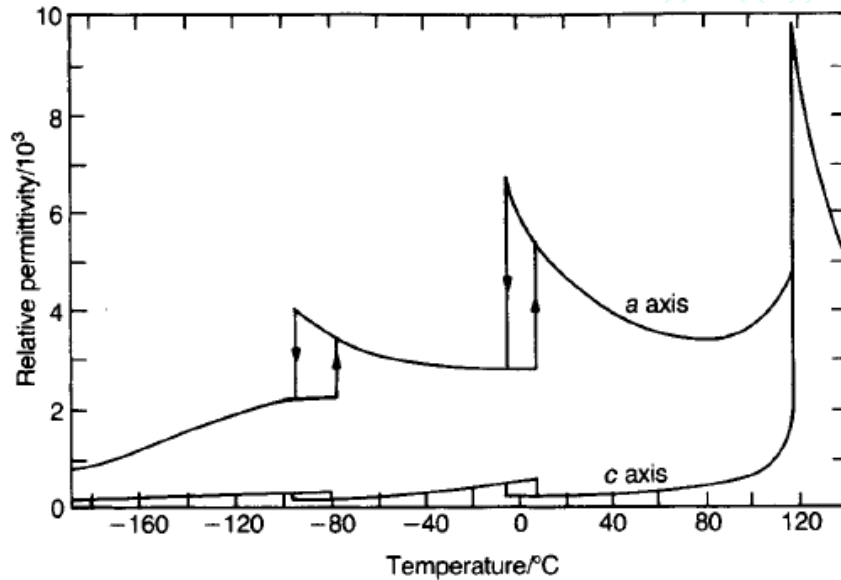
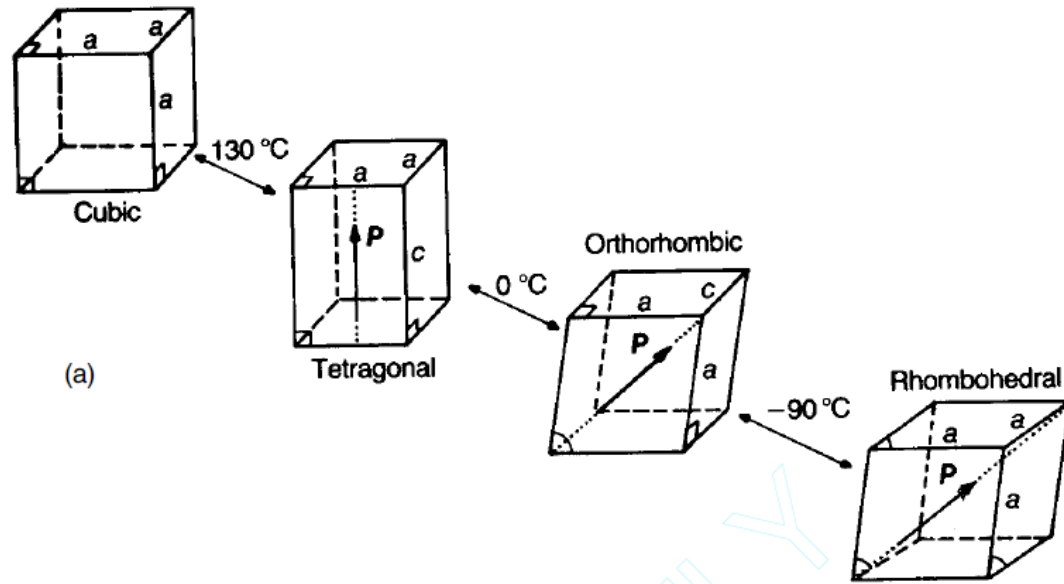
BaTiO₃: Cation displacement - second order Jahn-Teller distortion (or pseudo J-T distortion)

In the 1940s the dielectric and ferroelectric properties of BT were discovered. What is the reason for the spontaneous electric polarization in BT?

Ti⁴⁺ : d⁰ so it is not J-T ion. A symmetry change is provided by cation displacement along one of the symmetry axis of the octahedron (see slide 6).



BaTiO₃: phase transformation



Above T_c , BT shows a cubic structure. The tolerance factor is slight larger than 1 and distortions take place.

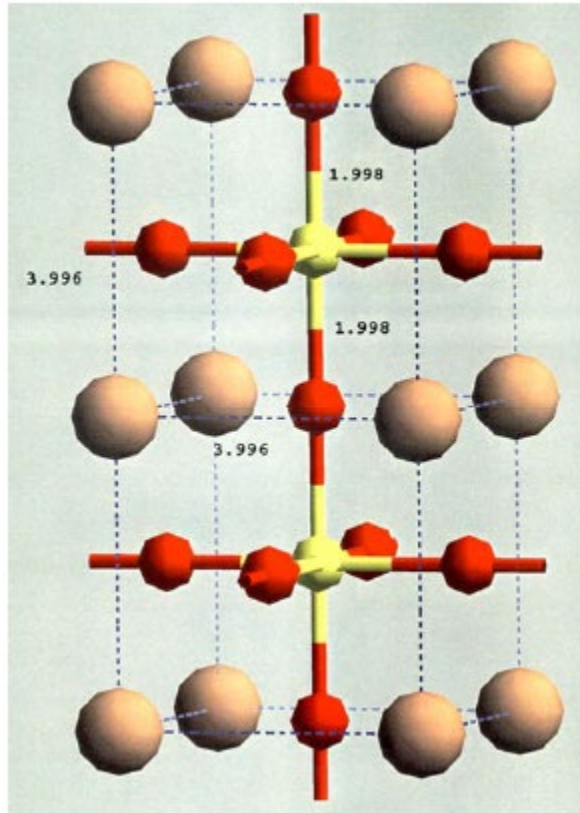
Table 2 Ionic radii and tolerance factors of the synthesised perovskite-type catalysts

Perovskite ABO ₃	Ionic radius [Å] ^{a,b}				Tolerance factor ^c
	Cation A		Cation B		
CaTiO ₃	Ca ²⁺ (VIII)	1.12	Ti ⁴⁺ (VI)	0.605	0.89
SrTiO ₃	Sr ²⁺ (XII)	1.44	Ti ⁴⁺ (VI)	0.605	1.00
BaTiO ₃	Ba ²⁺ (XII)	1.61	Ti ⁴⁺ (VI)	0.605	1.06
CaZrO ₃	Ca ²⁺ (VIII)	1.12	Zr ⁴⁺ (VI)	0.72	0.84
SrZrO ₃	Sr ²⁺ (XII)	1.44	Zr ⁴⁺ (VI)	0.72	0.95
BaZrO ₃	Ba ²⁺ (XII)	1.61	Zr ⁴⁺ (VI)	0.72	1.00
CaCeO ₃	Ca ²⁺ (VIII)	1.12	Ce ⁴⁺ (VI)	0.87	0.78
SrCeO ₃	Sr ²⁺ (XII)	1.44	Ce ⁴⁺ (VI)	0.87	0.88
BaCeO ₃	Ba ²⁺ (XII)	1.61	Ce ⁴⁺ (VI)	0.87	0.94

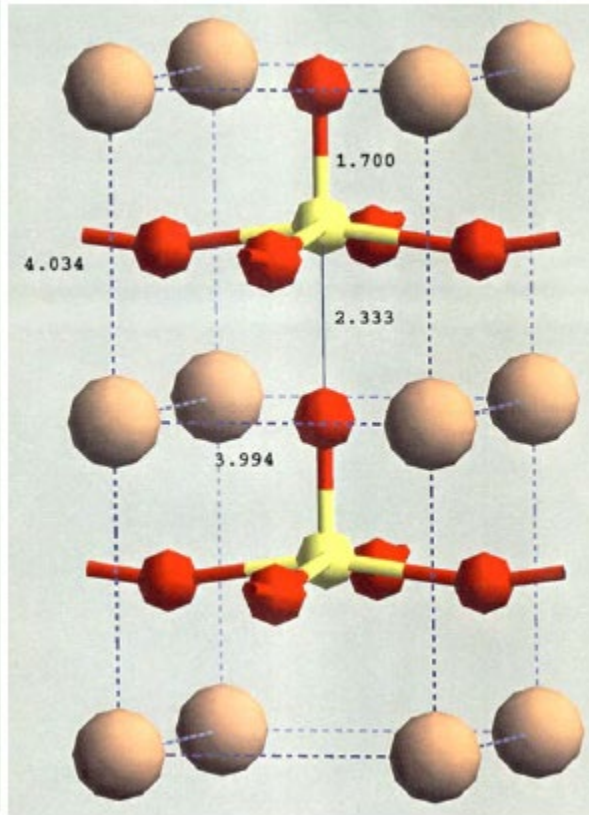
Cubic or tetragonal

^a Data from ref. 27. ^b Numbers in parentheses describe the coordination of the ion within the perovskite. ^c Ionic radius of O²⁻ (VI): 1.40 Å.

BaTiO₃: distortion



cubic

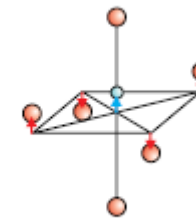


tetragonal

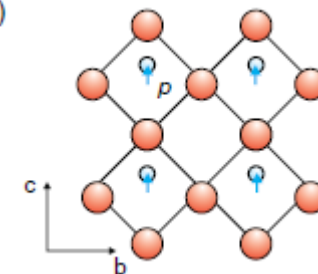
As for first order J-T distortion, also these are P sensitive in the GPa range.

As the crystal cools through the cubic – tetragonal transition temperature, the cubic cell expands slightly along one edge to produce the tetragonal *c*-axis and is slightly compressed along the other two edges to form the tetragonal *a*- and *b*-axes. The change in the Ba²⁺ positions is almost negligible. The Ti⁴⁺ displacement is accompanied by a slight change in octahedron dimensions so that two equatorial oxygen atoms move parallel to the +*c*-axis and two move in the opposite direction. These displacements give rise to electric dipoles, **p**, one in each octahedron that are the source of the ferroelectric properties of tetragonal BaTiO₃. There is no preference as to which of the original cubic axes becomes the polar direction, and so this can take one of six equivalent directions, so that a single crystal invariably becomes heavily twinned on cooling. Other distortion take place at lower temperature but without practical relevance.

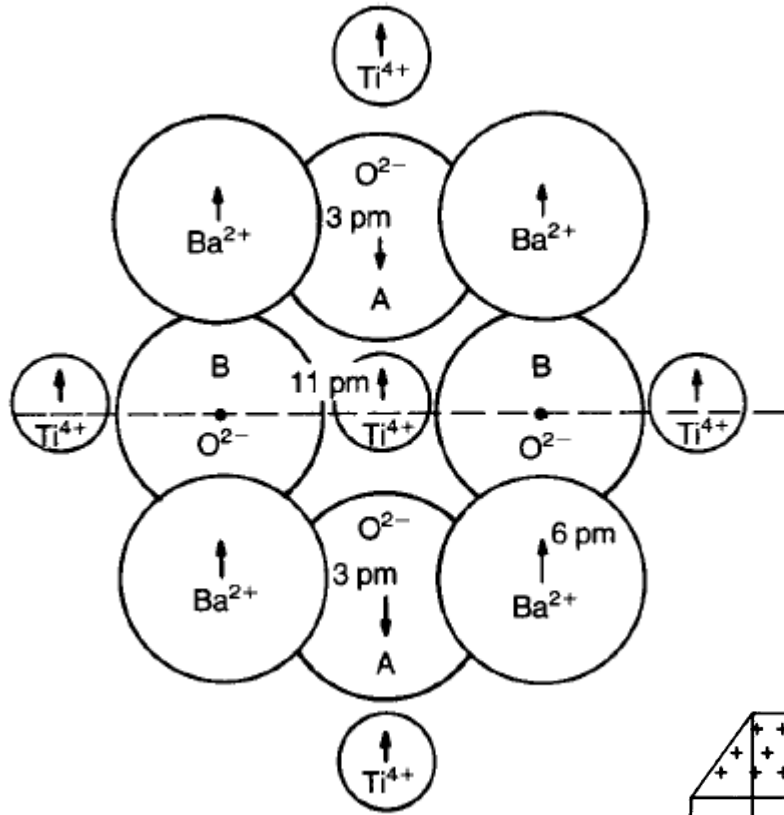
(c)



(d)

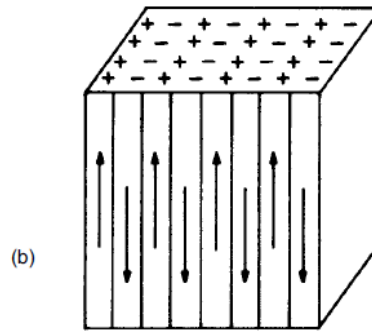
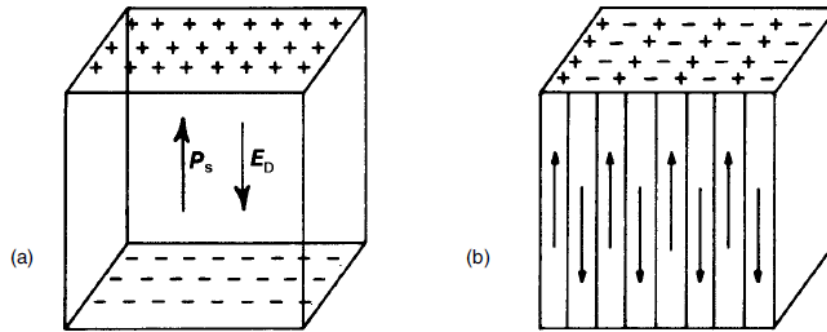


BaTiO₃: ferroelectric tetragonal structure.



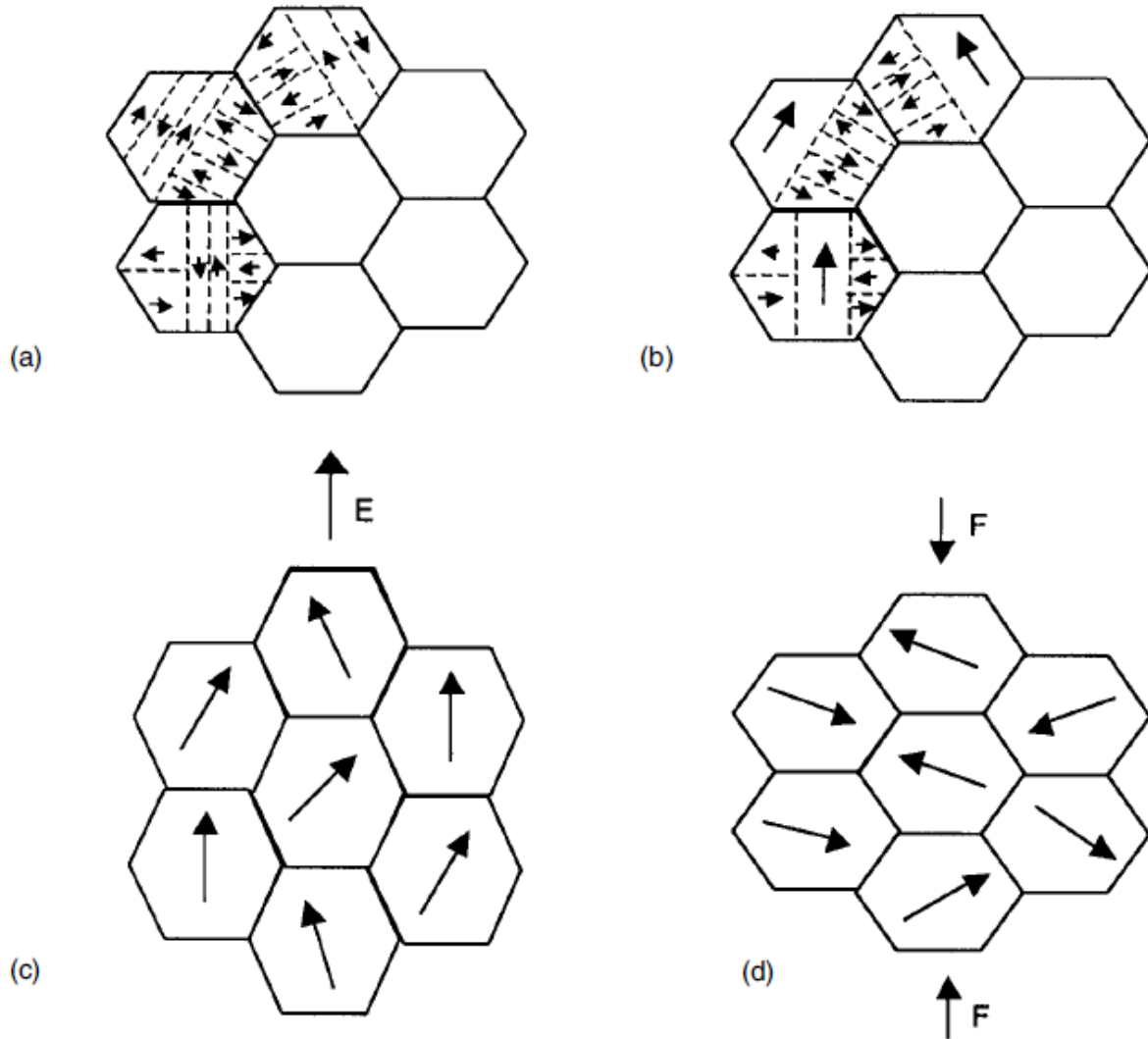
It is evident that if the central Ti⁴⁺ ion is closer to one of the O²⁻ ions marked A, it will be energetically favorable for the Ti⁴⁺ ion on the opposite side of A to be located more distantly from that O²⁻ ion, thus engendering a similar displacement of all the Ti⁴⁺ ions in a particular column in the same direction. Coupling between neighboring columns occurs in BaTiO₃ so that all the Ti⁴⁺ ions are displaced in the same direction.

An immediate consequence of the onset of spontaneous polarization in a body is the appearance of an apparent surface charge density and an accompanying depolarizing field ED (a).



The energy associated with the polarization in the depolarizing field is minimized by twinning, a process in which the crystal is divided into many oppositely polarized regions, as shown in (b). These regions are called domains and the whole configuration shown comprises 180° domains. Thus, the surface consists of a mosaic of areas carrying apparent charges of opposite sign, resulting in a reduction in ED and in energy.

BaTiO₃: ferroelectric domains



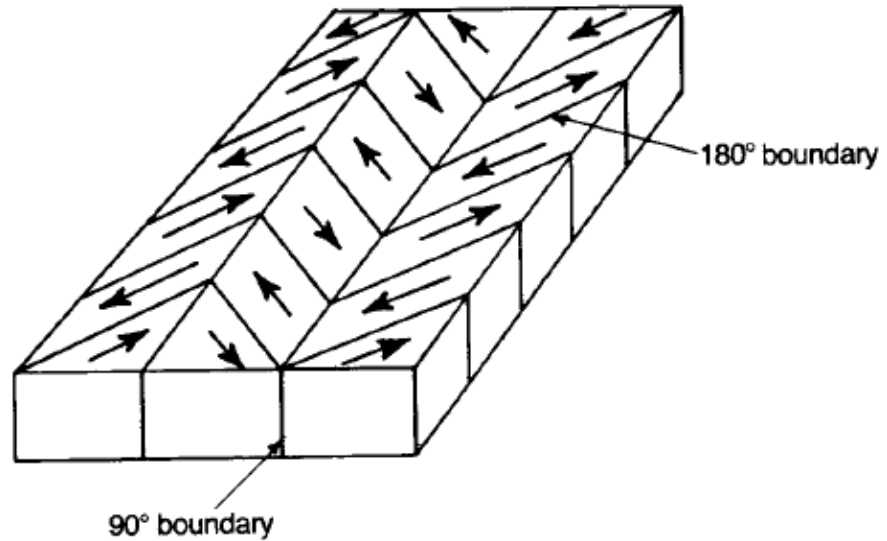
Schematic illustrating the changes accompanying the application of electrical and mechanical stresses to a polycrystalline ferroelectric ceramic:

- (a) stress-free – each grain is non-polar because of the cancellation of both 180° and 90° domains;
- (b) with applied electric field – 180° domains switch producing net overall polarity but no dimensional change;
- (c) with increase in electric field, 90° domains switch accompanied by small (1%) elongation;
- (d) domains disorientated by application of mechanical stress.

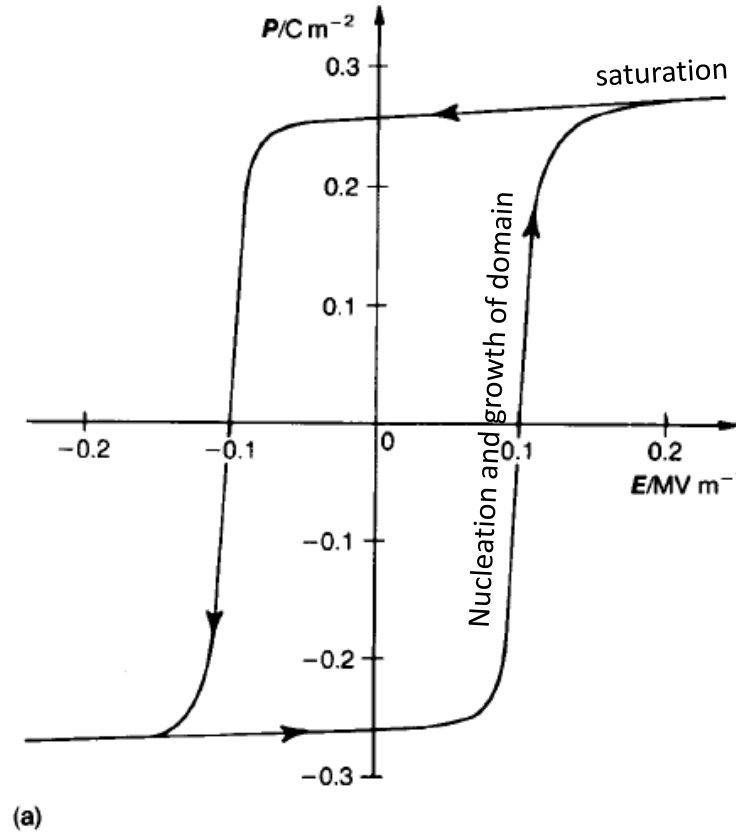


Polished and etched unpoled ceramic.

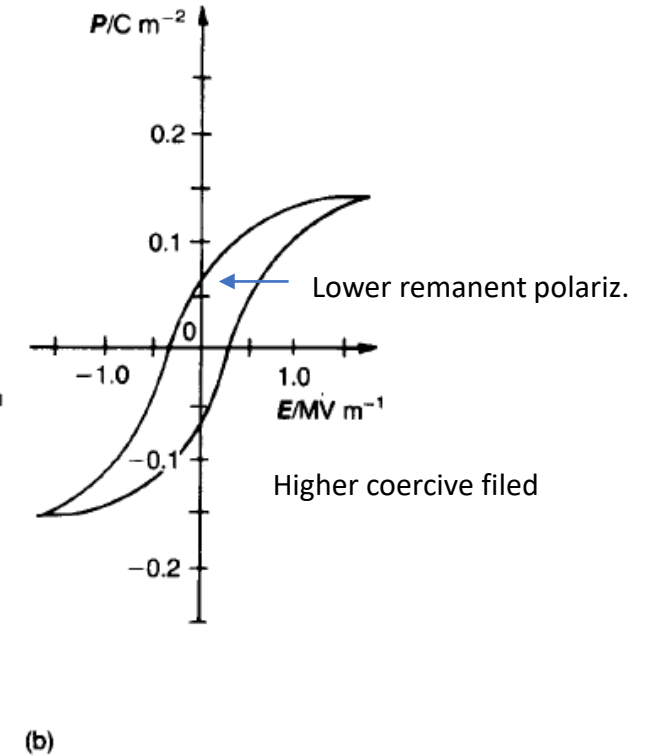
BaTiO₃: ferroelectric domains



Domain wall (≈ 10 nm)



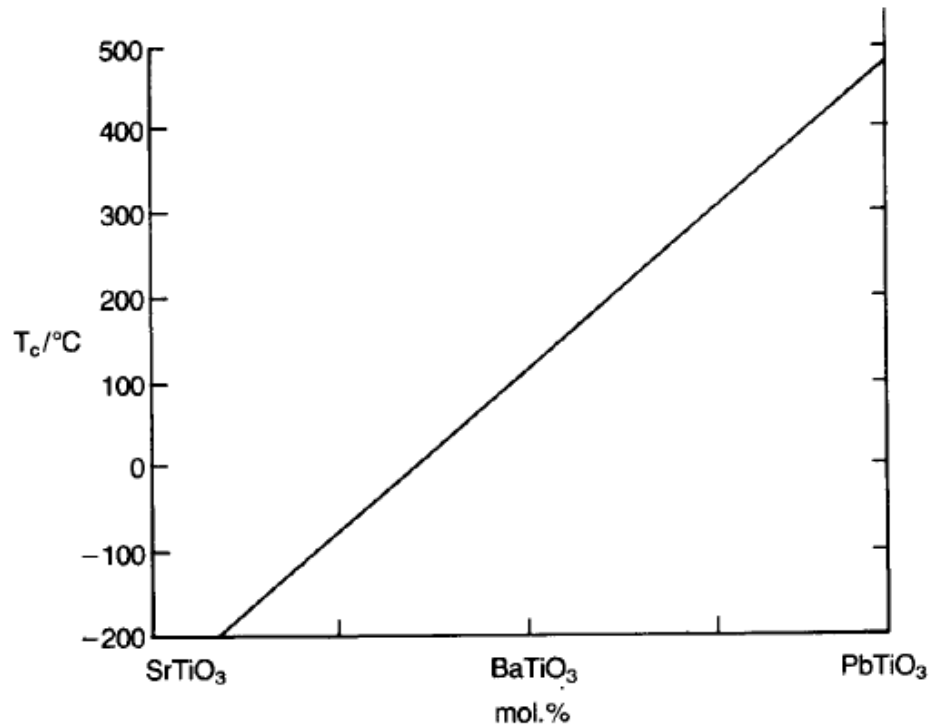
Single domain



Ceramics

The detailed geometry and dynamics of changes in domain configuration in a single crystal accompanying changes in applied field are complex and there is marked hysteresis between induced polarization and an applied field of sufficient strength. Conditions in a crystallite clamped within a ceramic are even more complex.

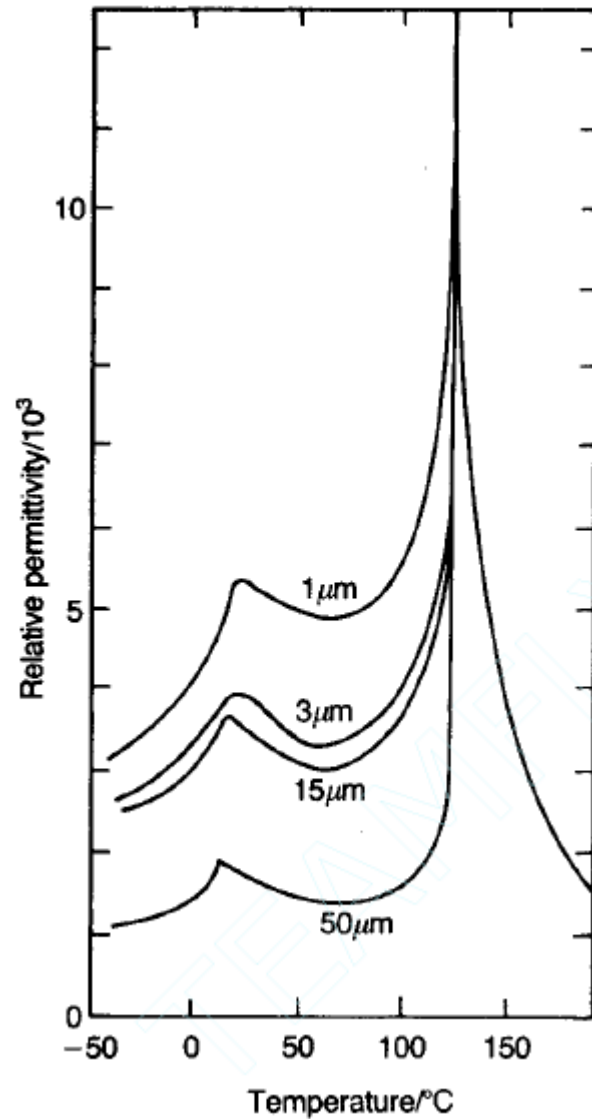
Tuning T_c



One very significant advantage of ceramic ferroelectrics is the ease with which their properties can be modified by adjusting the composition and the ceramic microstructure. Additions and the substitution of alternative cations can have the following effects:

1. shift the Curie point and other transition temperatures;
2. restrict domain wall motion;
3. introduce second phases or compositional heterogeneity;
4. control crystallite size;
5. control the oxygen content and the valency of the Ti ion.

Grain size effect



Cations that have a higher valency than those they replace, when present at levels exceeding about 0.5 cation percent, e.g. La^{3+} in place of Ba^{2+} or Nb^{5+} in place of Ti^{4+} , generally inhibit crystal growth. This has the effect of raising the permittivity level below the Curie point as shown in the figure. Crystal size is also controlled by sintering conditions. It has important effects on the electro-optical behavior.

Kröger–Vink defect notation

Table B.1 The Kröger–Vink notation for defects in crystals

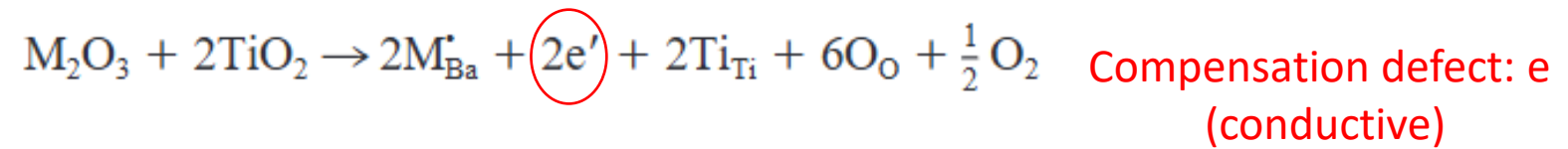
Defect type	Notation	Defect type	Notation
Metal vacancy at metal (M) site	V_M	Non-metal vacancy at non-metal (Y) site	V_Y
Impurity metal (A) at metal (M) site	A_M	Impurity non-metal (Z) at non-metal (Y) site	Z_Y
Interstitial metal (M)	M_i	Interstitial non-metal (Y)	Y_i
Neutral metal (M) vacancy	V_M^x	Neutral non-metal (Y) vacancy	V_Y^x
Metal (M) vacancy with negative effective charge	V_M'	Non-metal (Y) vacancy with positive effective charge	V_Y^*
Interstitial metal (M) with n positive effective charges	M_i^{n+}	Interstitial non-metal (Y) with n negative effective charges	Y_i^{n-}
Free electron	e'	Free hole	h^*
Neutral associated defects (vacancy pair)	$(V_M V_Y)$	Associated defects with positive effective charge	$(V_M V_Y)^*$

Examples:

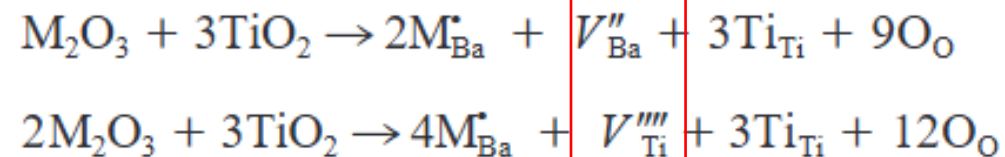
1. in SrTiO_3 , the symbol V_{Sr} would represent a strontium atom vacancy;
2. a Ba substituent on an Sr site in SrTiO_3 is written as Ba_{Sr}
3. O_i would represent an interstitial oxygen atom in $\text{La}_2\text{CuO}_{4+\delta}$
4. Associated lattice defects are in parentheses
5. The superscript ' is used for each unit of effective negative charge; the superscript • is used for each unit of effective positive charge: La substituent on an Sr site in SrTiO_3 would have an effective charge of +1 and be written La_{Sr}^+ . The charge balance would be maintained by the creation of a Ti^{3+} cation in place of a Ti^{4+} cation, written Ti_{Ti}'
6. Electrons and holes are denoted by the symbols e' and h^*
7. O_i'' would represent an interstitial O^{2-} anion in $\text{La}_2\text{CuO}_{4+\delta}$
8. A defect that has no effective charge can be given the (optional) superscript x

Ion incorporation in BT into A-site

The mechanism of dopant incorporation into BT has been extensively investigated and the behavior of some transition-metal ions as well as that of the larger rare-earth ions has been well elucidated. The ionic radius is the parameter which mainly determines the substitution site. La^{3+} (1.15 Å) and Nd^{3+} (1.08 Å) are exclusively incorporated at the Ba^{2+} (1.35 Å) site, as their size is incompatible with that of Ti^{4+} (0.68 Å). In fact, it has long been known that La^{3+} and Nd^{3+} , when added in small amounts (<0.5at.%), behave as **donors** and lead to room-temperature semiconducting ceramics (electron compensation) with positive temperature coefficient of resistivity (PTCR).



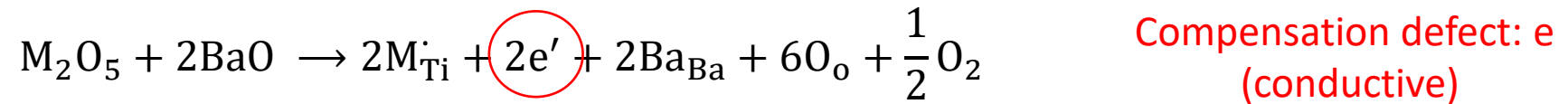
When the dopant concentration increases, the material becomes insulating, and the transition is accompanied by grain growth inhibition. In heavily doped materials, charge compensation takes place by barium (V''_{Ba}) or titanium (V''''_{Ti}) vacancies



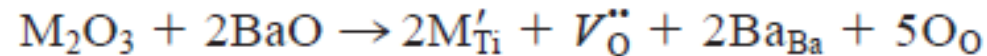
Compensation defect: V
(insulator)

Ion incorporation in BT into B-site

The transition series ions Cr^{4+} (0.55 Å), Fe^{3+} (0.64 Å), Co^{2+} (0.78 Å), Co^{3+} (0.63 Å), Mn^{2+} (0.83 Å), Mn^{3+} (0.64 Å), Mn^{4+} (0.53 Å), Ni^{2+} (0.78 Å), Nb^{5+} (0.64 Å), and Ta^{5+} (0.64 Å), because of their small size, give exclusive substitution on the Ti (B) site. In particular, Nb^{5+} is added as a **donor** in small concentrations (<0.3 at.%) to obtain semiconducting ceramics.

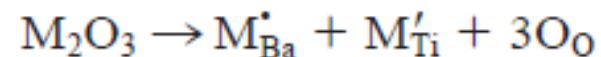


while Ni^{2+} , Co^{2+} , Co^{3+} , Fe^{3+} , and Mn^{2+} act as **acceptors** and give insulating materials at room temperature. The positive excess charge of the acceptor ion at the Ti site is mainly compensated by creation of oxygen vacancies (V_O'')



Ion incorporation in BT into A&B-sites

For Y^{3+} and lanthanide ions of intermediate size, from Sm^{3+} (1.04 Å) to Er^{3+} (0.96 Å), there are some indications that the substitution site is not exclusive, but is affected by dopant concentration, sintering temperature, sintering atmosphere, and Ba/Ti molar ratio (which play a major role). Self-compensation is possible.



These dopants are called “magic dopants”: since they can be incorporated in both sites can adjust small stoichiometry mismatch and increase in general the stability of the material.

Positive temperature coefficient resistors (PTCR)

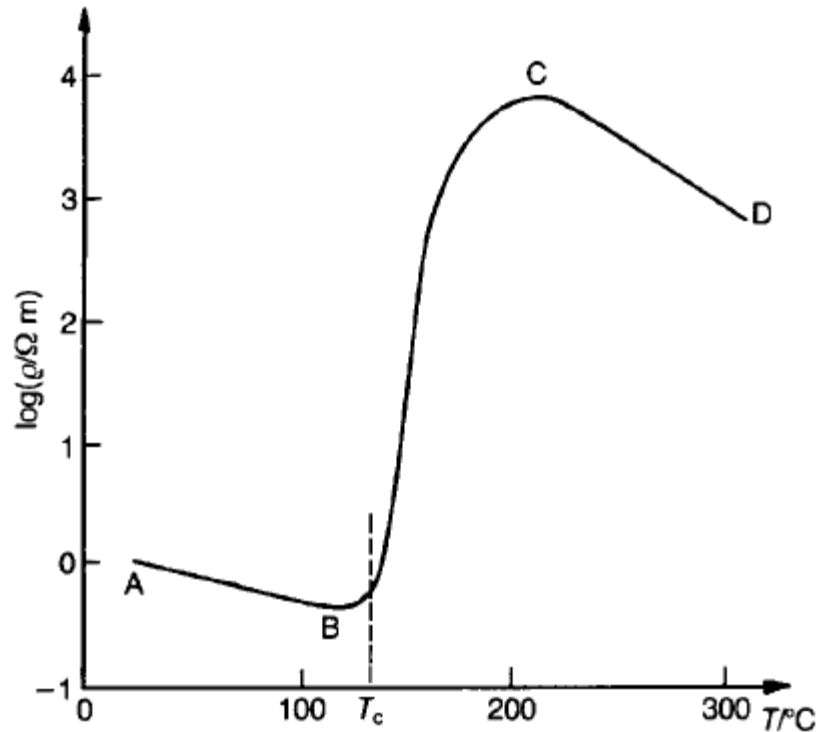


Fig. 4.20 Typical characteristic of PTC thermistor material.

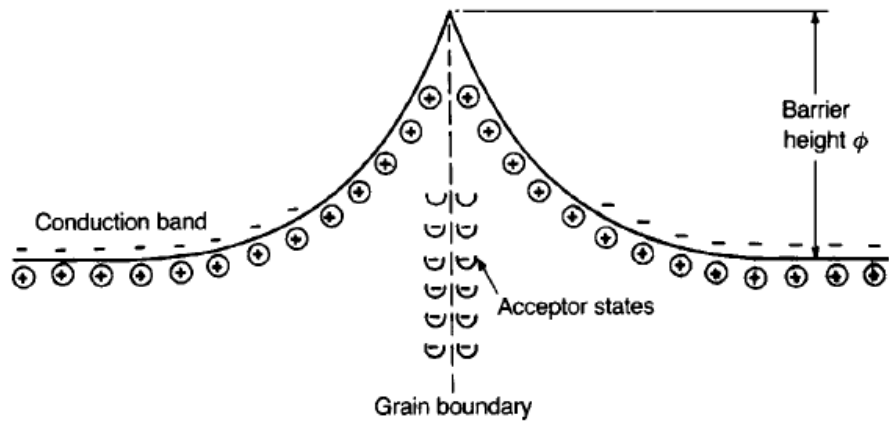
In the figure the material has the negative resistivity temperature characteristic associated with normal semiconductors up to about 100 °C (AB) and above about 200 °C (CD), while between these temperatures (BC) there is an increase of several orders of magnitude in resistivity.

The PTC effect is exhibited by specially doped and processed BaTiO_3 . Because the effect is not observed in the single-crystal form of the material, its cause must be assumed to lie in processes associated with grain boundaries. Attention here is focused on lanthanum-doped BaTiO_3 (BLT), although other donor dopants would be satisfactory, e.g. yttrium (A site) or niobium, tantalum or antimony (B site).

Positive temperature coefficient resistors (PTCR)

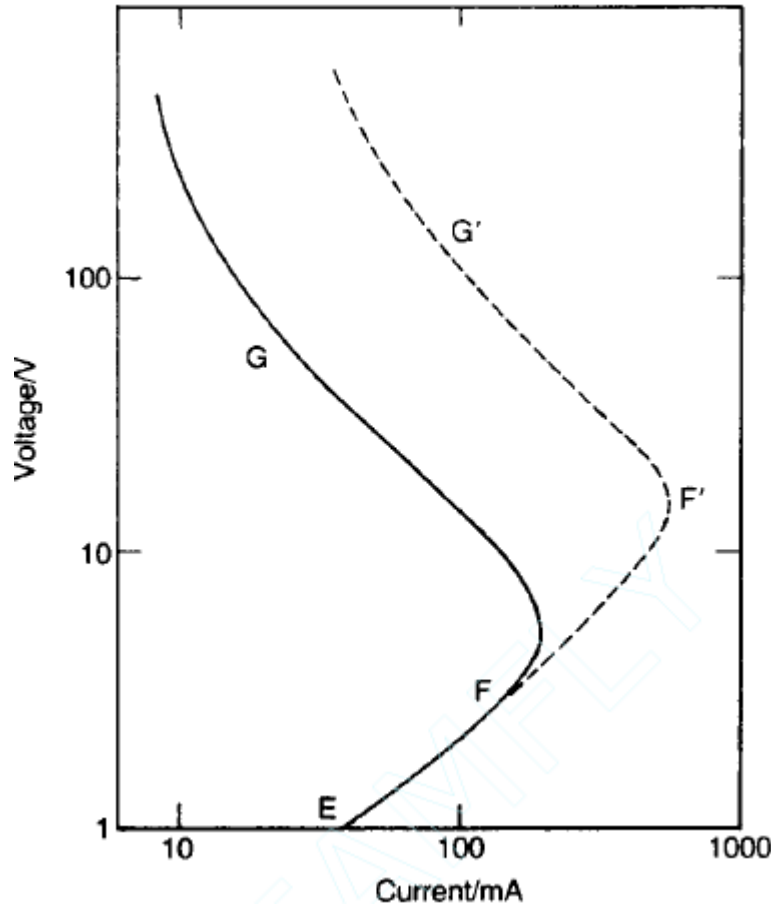
Electron acceptor states in the grain boundary together with nearby ionized donor states give rise to an electrical double layer.

Thus, conduction band electrons moving up to a grain boundary from the interior of a grain are confronted by a potential barrier of height ϕ



The PTC effect is seen to have its origins in the resistance of the grain boundary region which increases exponentially with temperature above the ferroelectric–paraelectric transition temperature. It therefore depends on the number of grain boundaries per unit volume of ceramic, i.e. on the microstructure, and of course on the acceptor and donor state densities.

Current voltage behavior of a PTCR body

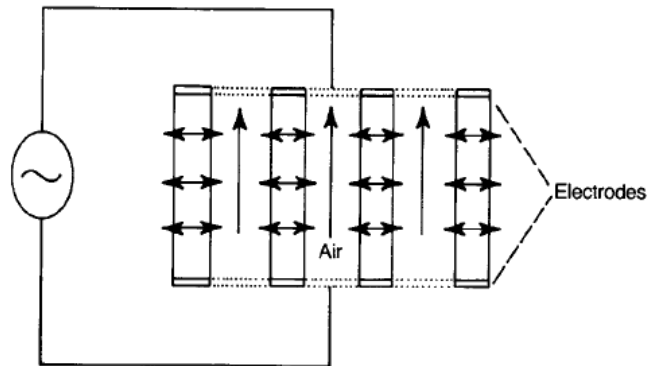


At low voltages (EF) the relation is approximately ohmic (Fig. 4.20, AB); then, as the temperature of the thermistor reaches the regime of steeply rising resistance (Fig. 4.20, BC), its temperature rises only slowly with increasing voltage and the current falls to give a correspondingly slow increase in power dissipation. If the increase in voltage is sufficient to bring the temperature above the region of rising resistance (Fig. 4.20, CD), the temperature coefficient becomes negative and a rapid increase in current and temperature results.

If the rate of heat dissipation from the thermistor is changed, the location of FG will shift. The temperature of the element changes only slightly, but the power changes to a level corresponding to the new rate of heat dissipation. If the voltage is kept constant the current becomes a measure of the rate of heat dissipation, and this relation is used in a number of devices to sense a change in environment. There is a marked change in heat dissipation when a probe at thermal equilibrium in air is plunged into a liquid at the same temperature as the air. Devices for indicating the level of liquids in tanks are based on this change.

Ohmic: $R = V/I$

PTCR as heating elements or sensor



The relative constancy in the temperature of a PTC device, despite changes in both the voltage supply and ambient conditions, when it is maintained on the steeply rising limb of its resistance–temperature characteristic has led to its use as a heating element in miniature ovens for quartz crystals acting as constant frequency sources. It has also been made use of in hair-driers and space-heaters.



PTCR kit

Air is blown through the perforations in a block of ceramic that is designed to heat the emergent air to a suitable temperature. Even when the fan is switched off the heater temperature only rises by about 20 °C so that no damage results.

PTC elements make useful temperature indicators because the sharp rise in resistivity above the Curie point is very easily detected or used to operate a control mechanism.

PTCR for automotive

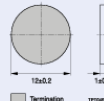



Sample Kit
PTC Thermistors
Heating elements
for low voltage applications



www.tdk-electronics.tdk.com



PTC Thermistors – Heating elements for low voltage applications									
Type	T ₉₀ (typ.) °C	R ₉₀ (V = V ₀) Ω	T ₉₀ ¹⁾ (V = V ₀) °C	R ₉₀ (V _{max} ≤ 1.5 V) Ω	V ₀	Curvature mm	Ordering code	Dimensional drawing	
V _{max} = 30 V DC, V ₀ = 12 V DC									
A60	40	4 ²⁾	70	9 ±30%	> 36	< 0.2	B59060A0040A010		mm
A60	60	5	80	9 ±30%	> 36	< 0.2	B59060A0060A010		
A60	80	4	95	9 ±30%	> 36	< 0.2	B59060A0080A010		
A60	120	4	140	9 ±30%	> 36	< 0.2	B59060A0120A010		
A60	160	3	165	9 ±30%	> 36	< 0.2	B59060A0160A010		
A60	180	3	185	9 ±30%	> 36	< 0.2	B59060A0180A010		
V _{max} = 24 V DC, V ₀ = 12 V DC									
R41	80	1.00	110	3.2 ±50%	> 40	< 0.05	B59041R0080A010		mm
R41	120	1.00	145	3.2 ±50%	> 40	< 0.05	B59041R0120A010		
R41	160	0.75	180	3.2 ±50%	> 40	< 0.05	B59041R0160A010		
R41	180	0.75	200	3.2 ±50%	> 40	< 0.05	B59041R0180A010		
R41	220	1.00	230	6.4 ±50%	> 40	< 0.05	B59041R0220A010		
V _{max} = 60 V DC, V ₀ = 48 V DC									
R210	150	18.00	175	30 typical	> 120	< 0.05	B59210R0150A010		
1) Measured between points 2) T (R ₉₀ = R ₀) < 25 °C									
Data sheets are available at: www.tdk-electronics.tdk.com/ptc_heating								Content: 3 pcs per ordering code	
Important information: It is incumbent on the customer to check and decide whether a product is suitable for use in a particular application. Our products are described in detail in our data sheets. Our important notes and the product-specific Caution and warnings must be observed. All relevant information is available through our sales offices.									
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Co-firing example: 5 layers active component

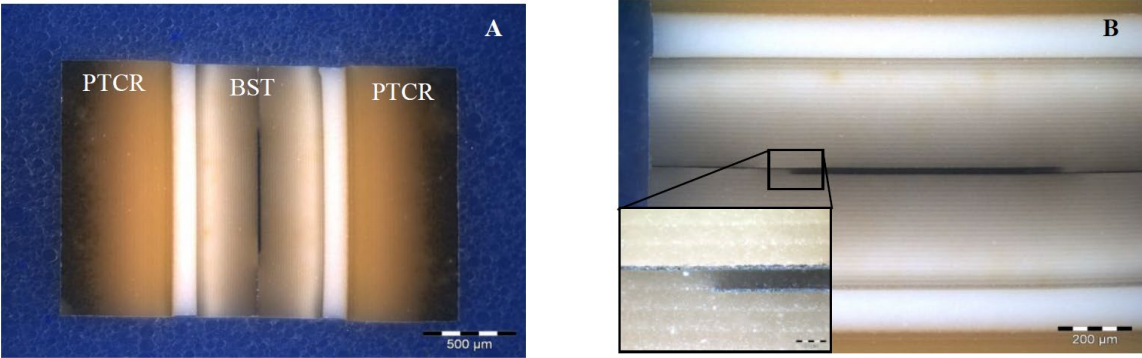


Figure 3 – Device cross sections: (A) overall view, (B) magnification of the inner electrodes’ area.

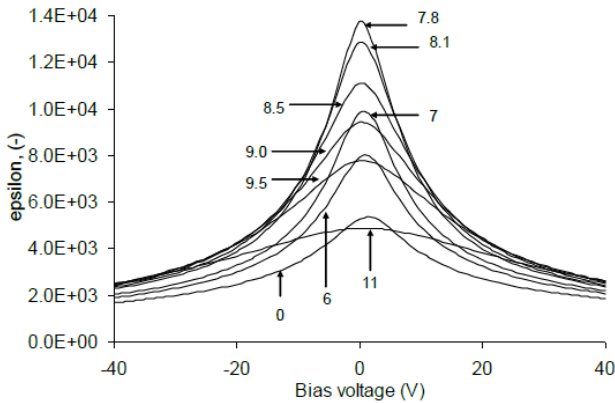


Figure 5 – Dielectric permittivity against Bias_V at different PTC_V (Frequency 200 KHz)

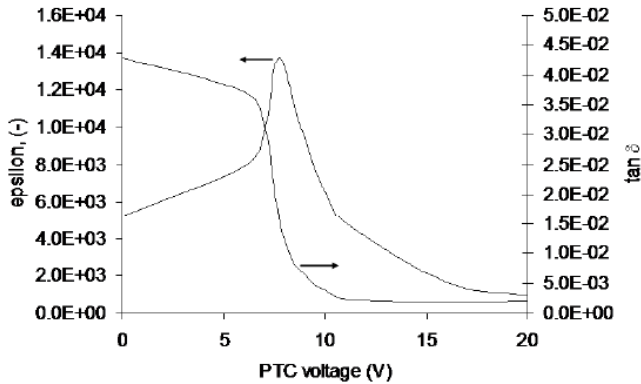
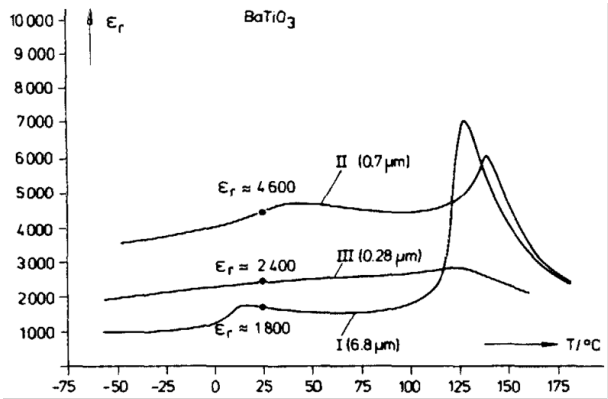
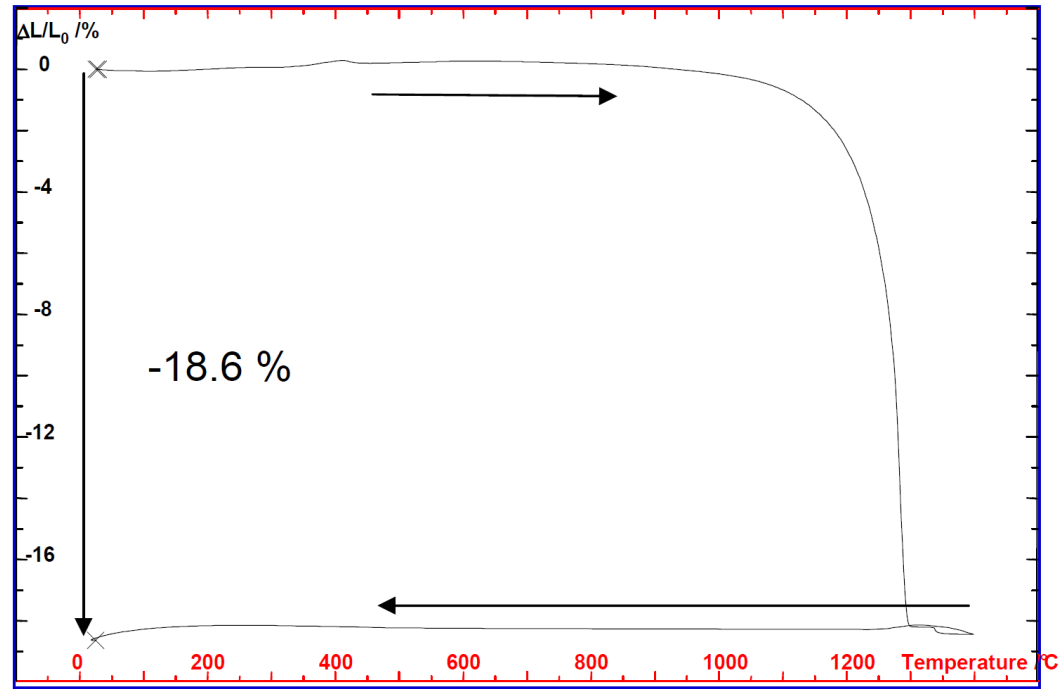


Figure 4 – Dielectric permittivity and dielectric loss against the PTC_V (Frequency 200 KHz)



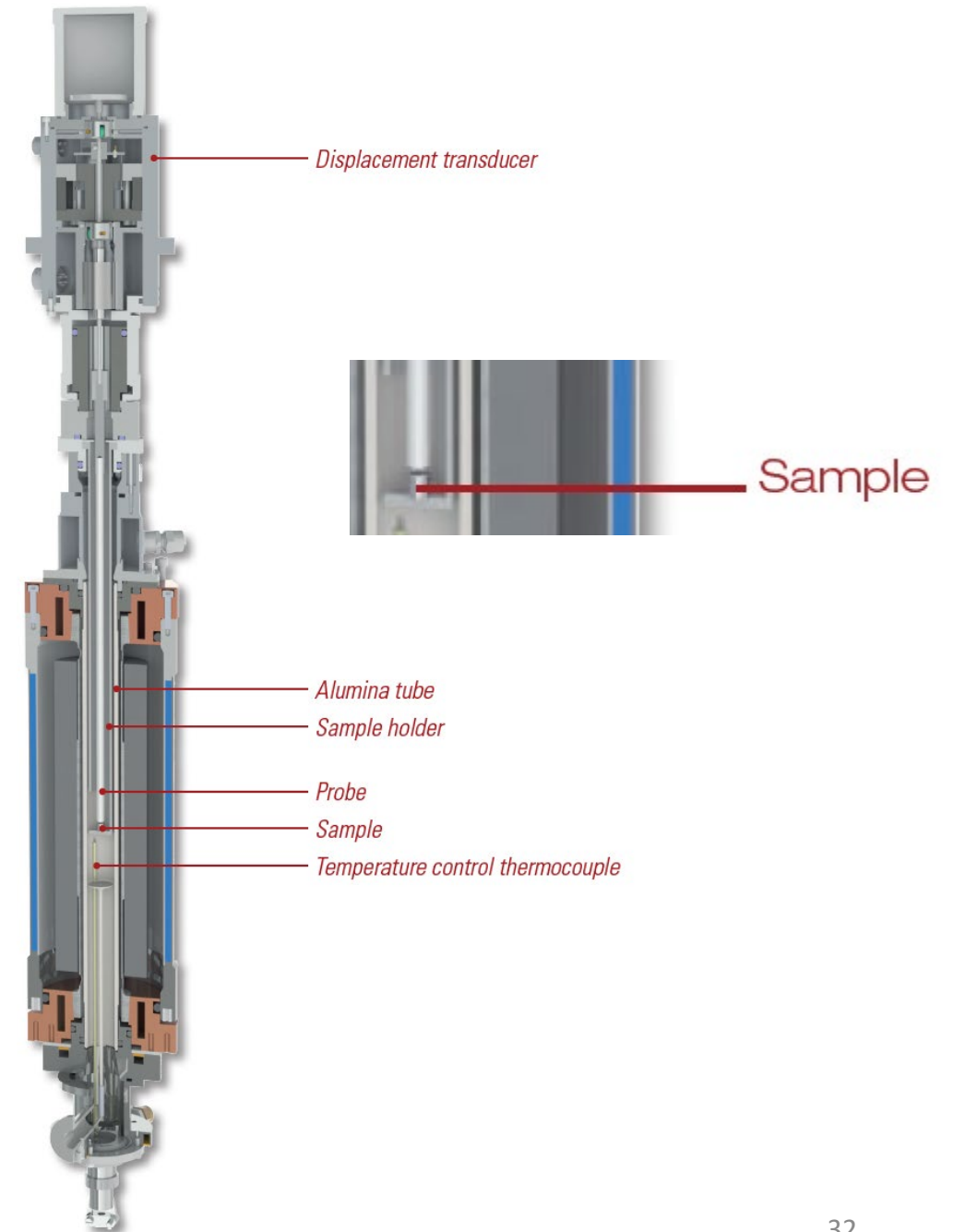
Dielectric constant vs. temperature of BaTiO₃ ceramic showing various grain sizes

Thermomechanical analysis (TMA) / Dilatometry

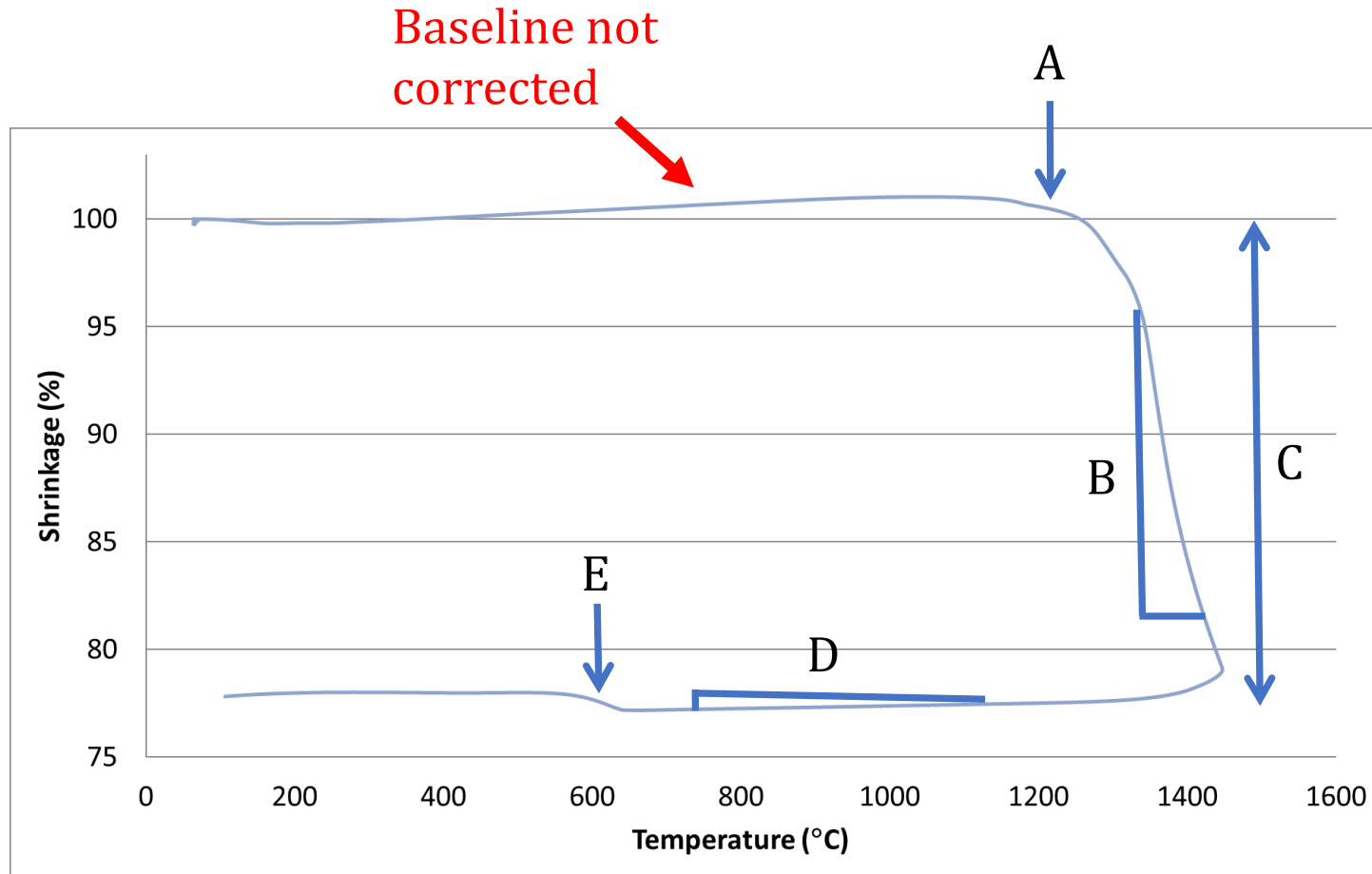


Controlled sintering rate

Properties of a material are improved by maintaining a constant and slow rate of shrinkage during the sintering process. Key parameters are maximum heating rate and sintering rate. The heating rate can be automatically lowered to follow predefined sintering rate and reincreased at the end of the process. This mode is used to generate an optimized temperature profile and to simulate the sintering process.



Co-firing: key (starting) points



- A: sintering onset
- B: shrinkage speed
- C: overall shrinkage
- D: thermal expansion on cooling
- E: eventually, phase transitions

A...E: parameters have to match between materials to be co-fired.
No match → cracks, delamination, failure

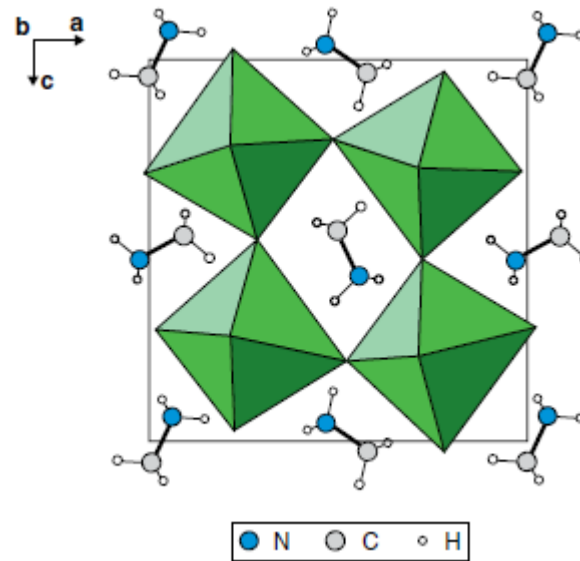
Hybrid Organic-Inorganic Perovskites

Table 1.6 Organic-inorganic hybrid and related perovskites

Phase	Space group	a (nm)	b (nm)	c (nm)	Angles (°)	Cubic transition Temp (K)
CsSnI ₃	O, <i>Pnma</i> (62)	0.86885	1.23775	0.86384		300
CsSnI ₃	T, <i>P4/mbm</i> (127)	0.87182		0.61908		350
CsSnI ₃	C, <i>Pm3m</i> (221)	0.62057				478
MAGeCl ₃	M, <i>P2₁/n</i> (14)	1.09973	0.72043	0.82911	α , 90.47	2
MAGeCl ₃	O, <i>Pmna</i> (62)	1.11567	0.73601	0.82936		250
MAGeCl ₃	Tr, <i>R3m</i> (160)	0.56784			α , 90.95	370
MAGeCl ₃	C, <i>Pm3m</i> (221)	0.56917				475
CD ₃ ND ₃ GeCl ₃	M, <i>P2₁/n</i> (14)	1.09973	0.72043	0.82911	β , 90.47	2
CD ₃ ND ₃ GeCl ₃	O, <i>Pnma</i> (62)	1.11567	0.73601	0.82936		250
CD ₃ ND ₃ GeCl ₃	Tr, <i>R3m</i> (160)	0.56584			α , 90.95	370
CD ₃ ND ₃ GeCl ₃	C, <i>Pm3m</i> (221)	0.56917				475
MASnCl ₃	Tri, <i>P1</i> (1)	0.5726	0.8227	0.7910	α , 90.40 β , 93.08 γ , 90.15 β , 93.03 α , 91.90	297
MASnCl ₃	M, <i>Pc</i> (7)	0.5718	0.8326	0.7938		318
MASnCl ₃	Tr, <i>R3m</i> (160)	0.5734				350
MASnCl ₃	C, <i>Pm3m</i> (221)	0.5760				478
MASnBr ₃	O, <i>Pmc2₁</i> (26)	0.58941	0.83862	0.82406		215
MASnI ₃	T, <i>P4mm</i> (99)	0.62302		0.6231		293
MASnI ₃	T, <i>I4cm</i> (108)	0.87577		1.2429		200
MAPbI ₃	T, <i>P4mm</i> (99)	0.63115		0.63161		400
MAPbI ₃	T, <i>I4cm</i> (108)	0.8849		1.2642		293
MAPbI ₃	O, <i>Pmna</i> (62)	0.88362	1.25804	0.85551		100
FASnI ₃	O, <i>Amm2</i> (38)	0.63286	0.89554	0.89463		340
FASnI ₃	O, <i>Imm2</i> (44)	1.25121	1.25171	1.25099		180
CH ₃ ND ₃ PbCl ₃	O, <i>Pnma</i> (62)	1.11747	1.13552	1.12820		80
CH ₃ ND ₃ PbCl ₃	C, <i>Pm3m</i> (221)	0.5669				280
CH ₃ ND ₃ PbBr ₃	O, <i>Pnma</i> (62)	0.79434	1.18499	0.85918		11
MAPbI ₃	O, <i>Pnma</i> (62)	0.88362	1.25804	0.85551		100
MAPbI ₃	T, <i>I4/mcm</i> (140)	0.8851		1.2444		298
MAPbI ₃	C, <i>Pm3m</i> (221)	0.6274				333
FAPbI ₃	Tr, <i>P3m1</i> (156)	0.89817		1.1006	γ , 120	293

The A-sites in the perovskite structure are large enough to accommodate a number of complex ions including ammonium (NH₄)⁺; methyl ammonium (CH₃NH₃)⁺ frequently written as MA; tetramethylammonium, [(CH₃)₄N]⁺, frequently written as TMA and formamidinium (NH₂=CHNH₂)⁺, written as FA.

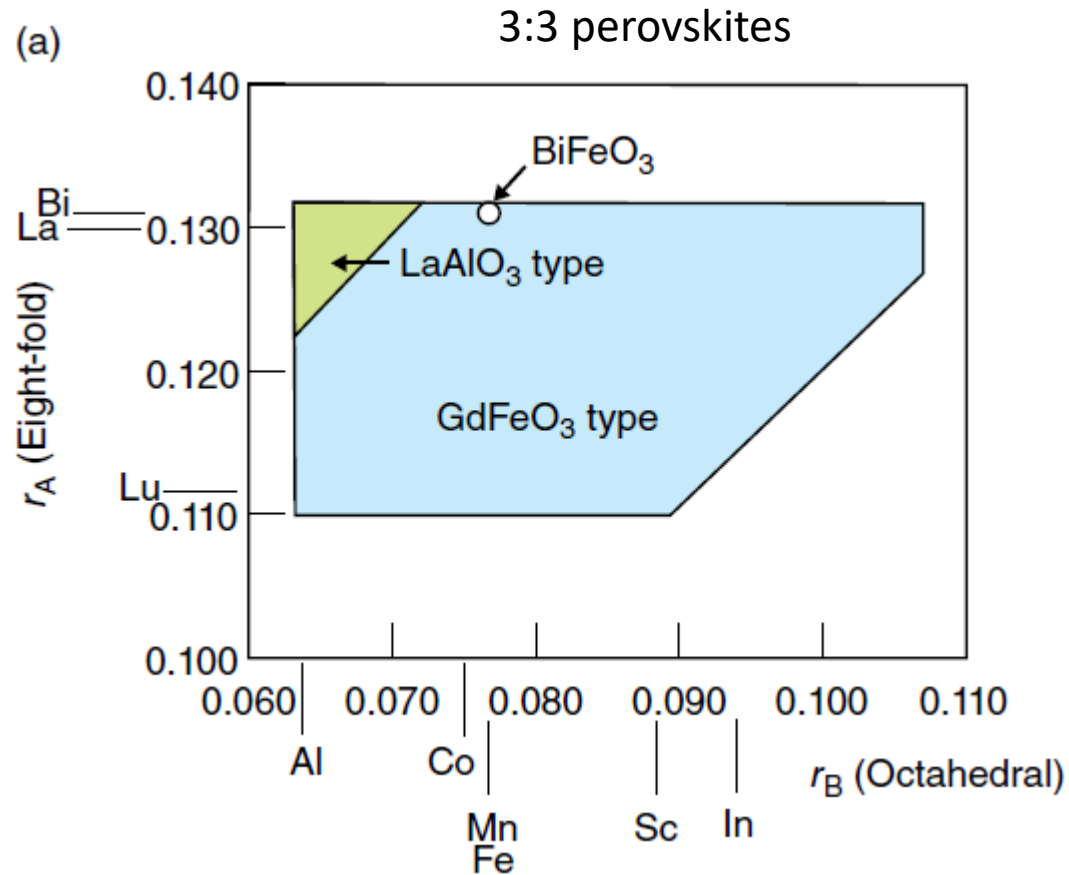
The most important of these are the compounds formed with the Group 14 elements Ge, Sn and Pb, together with a halogen Cl, Br and I.



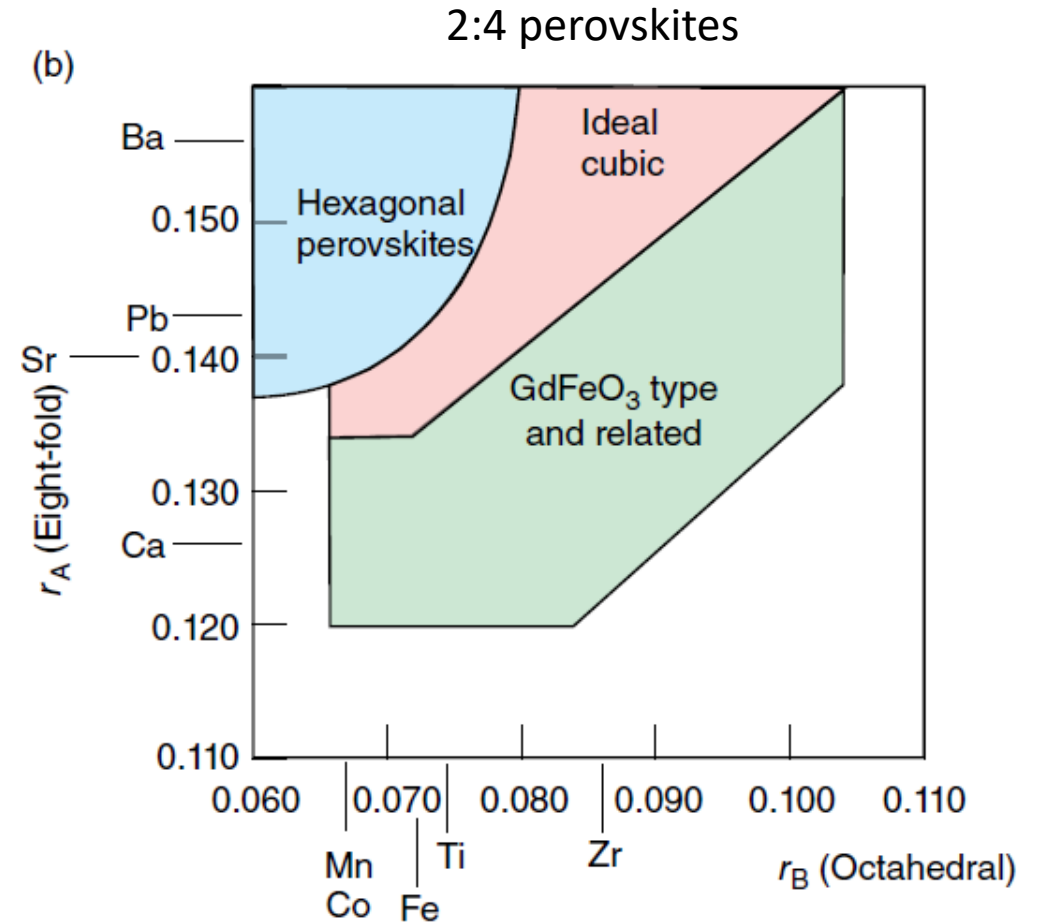
The structure of (MAPbCl₃). One layer of the structure is shown. In preceding and succeeding layers, the organic molecules are rotated by 180° compared to that drawn.

This class of materials is well-known for the assembly of perovskite solar cell (https://en.wikipedia.org/wiki/Perovskite_solar_cell)

Structure-Field Maps (related to the tolerance factor)



LaAlO₃ : trigonal
 GdFeO₃ : orthorhombic
 BiFeO₃ : rhombohedral (anomaly)

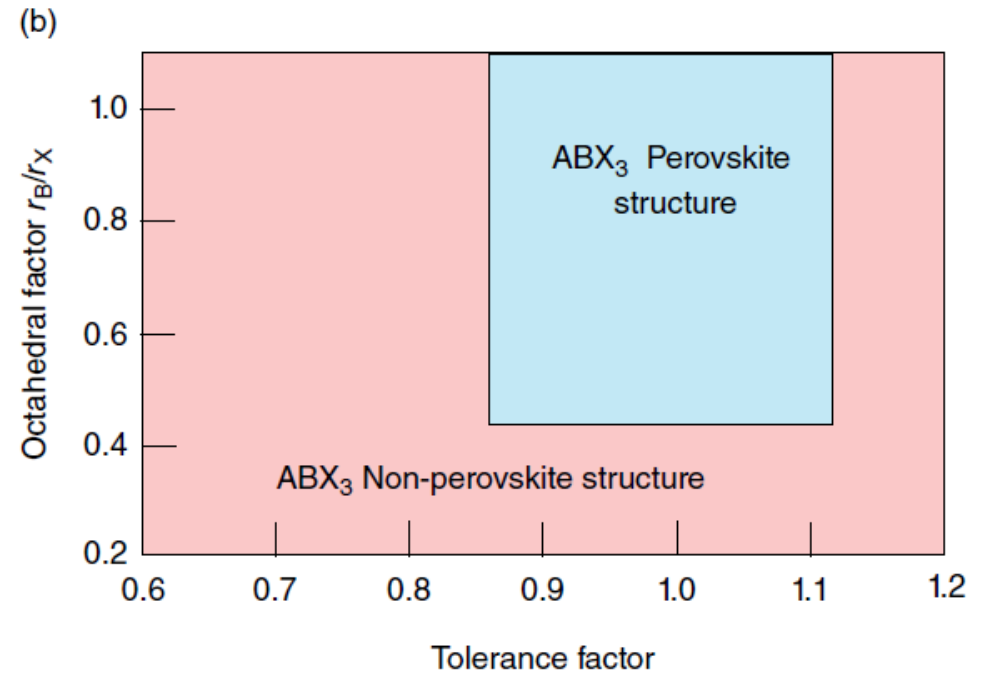
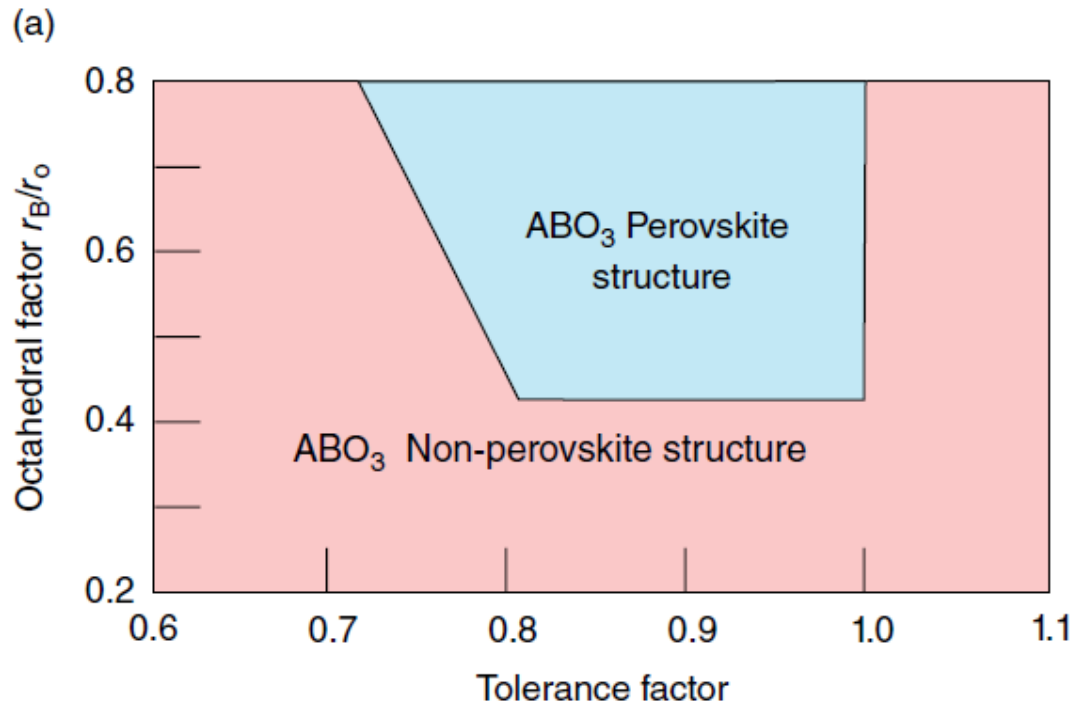


The radii appropriate to the y-axis, associated with the A cations, should refer to 12-fold coordination. As such radii are not widely available, the figures here use eightfold radii on this axis.

Perovskite vs. non-perovskites

Recent efforts have used plots of the tolerance factor against the ratio of the radii of the B-site cation to the X-site anion as an octahedral factor (μ) :

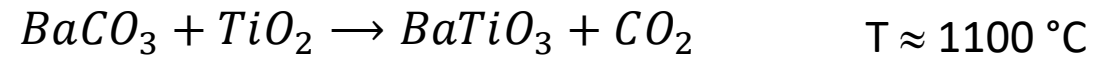
$$\mu = \frac{r_B}{r_X} \quad \text{radii of the B-site cation to the X-site anion}$$



Although structure-field maps do not predict the existence of the perovskite form with complete certainty, indicating that the factors that endow stability to this structure lie outside of simple radius correlations, the ease of the method makes it a simple and useful guide when unknown systems are being explored.

Perovskite: BT synthesis as example

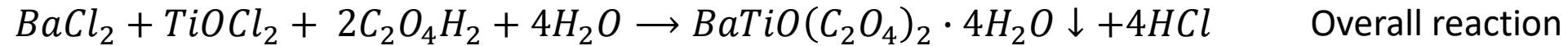
1. “Mixed oxide” or solid-state route



In case of NPs, T can be decreased to 700 °C [1]
obtaining ceramic BT with size $\approx 70\text{ nm}$ (!)

Advantages: easy, large scale, very well established. But: relatively high T, milling needed to obtain an average size $\approx 1\text{ }\mu\text{m}$

2. Oxalate route

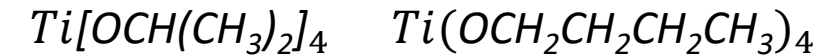
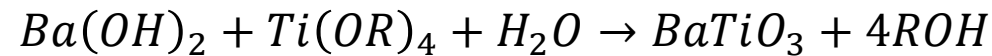


Advantages: lower T, smaller particle. But: care need to be taken during thermal treatment

Perovskite: BT synthesis as example

3. Alkoxide route

Different alkoxide can be used, typically isopropoxide, butoxide



In general $Ti(OR)_4$

The reaction can be strongly exothermic, additional mineralized (NaOH) might be used. Small particles can be produced, but relatively high-cost precursors. Butoxide route very interesting and largely tested. Very often a post-treatment is needed, such as a calcination step at relatively low temperature to convert the material into fully crystalline BT. This treatment induce a certain degree of aggregation. Gently milling would be required.

4. Hydrothermal route

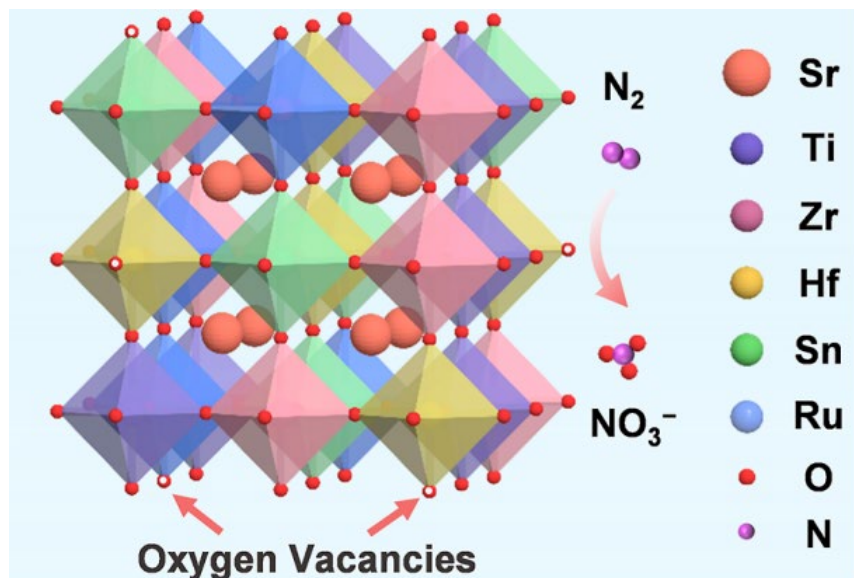
It is a relatively low-temperature method (100-250 °C) but autoclaves are needed (close pressured reactor). The pressure is typically the autogenous pressure generated in a closed reactor. Essentially, a Ba salt (such as chloride), a Ti precursor (such as $TiOCl_2$) and a mineralizer (such as NaOH) are mixed in a reactor and let react under hydrothermal conditions for few hours. The quality of the material obtained strongly depends on the experimental conditions, but it is typically well crystallized, and no thermal treatment is required.



$$100 > T (^{\circ}C) > 250 \quad 1 < P (bar) < 30 \quad pH > 12$$

An excess of mineralizer is needed to set the alkaline pH, which partially remain in the product (e.g., Na contamination)

High entropy perovskites, HEP (high entropy alloy, HEA)

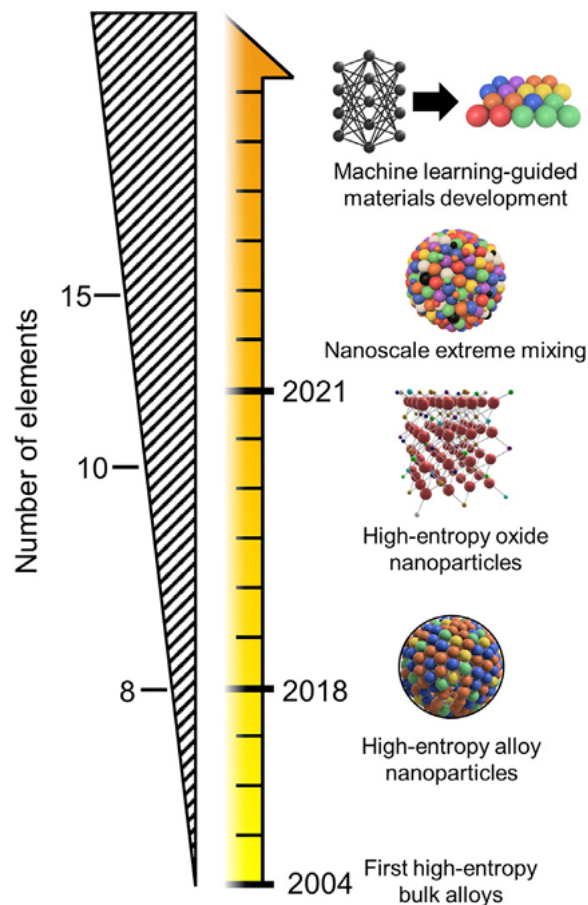


ACS Nano 2024, 18, 17642–17650

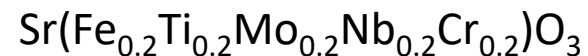
Joule 7, 843–854, May 17, 2023

ACS Sustainable Chem. Eng. 2020, 8, 17022–17032

A History of high entropy materials



Consider for instance the example



5 cations on B-site, equal amount

$$t = \frac{r_A + r_O}{\sqrt{2}(r_B + r_O)} = \frac{r_{\text{Sr}} + r_{\text{O}}}{\sqrt{2}\left(\frac{r_{\text{Fe}} + r_{\text{Ti}} + r_{\text{Mo}} + r_{\text{Nb}} + r_{\text{Cr}}}{5} + r_{\text{O}}\right)}$$

= 0.906

Adapted t factor

A cubic phase is likely to be stable when $0.9 \leq t \leq 1$, while an orthorhombic or rhombohedral phase may form when $t < 0.9$, and a tetrahedral or hexagonal phase may form when $t > 1$. From the calculated tolerance factor, it is apparent that the stable cubic HEP crystal structure could be formed

High entropy perovskites

Configuration entropy:

$$\Delta S_{conf} = -R \left[\left(\sum_{i=1}^N x_i \ln(x_i) \right)_{cation-site} + \left(\sum_{j=1}^M x_j \ln(x_j) \right)_{anion-site} \right]$$

Reduced to:

$$\Delta S_{conf} = -R \left[\left(\sum_{i=1}^N x_i \ln(x_i) \right)_{B-site} \right] \quad \text{in } A(x_i)O_3$$

Being $G = H + TS$ an increase of entropy due to the configurational contribution, leads to a thermodynamic stabilization. HEPs can therefore maintain negative values of G at high sintering temperatures, preventing phase transitions during cooling and forming energetically stable single-phase structures. These stable structures exhibit exceptional chemical and structural stability, making them highly suitable for energy applications.